

# Formation of massive stars: a review

Patrick Hennebelle

Thanks to: Benoît Commerçon, Marc Joos, Andrea Ciardi  
Gilles Chabrier, Romain Teyssier

# How massive stars form ?

- Can we form massive stars in spite of the radiative pressure ?
  - 1D: grain solution
  - 2D: flashlight solution
  - 3D: radiative instability solution
  - collision model
  
- Can we prevent the gas to fragment in many objects ?
  - isothermal
  - radiative feedback
  - magnetized non-radiative
  - radiative and magnetized
  
- Where the gas is coming from ?
  - competitive accretion
  - gravitational well based theory
  - tracing the gas in simulations

## Thermal Support

Consider a cloud of initial radius R

**If  $\gamma < 4/3$ , when R decreases,  $E_{therm}/E_{grav}$  decreases:**

=> heating/cooling processes

$$\frac{E_{therm}}{E_{grav}} = \frac{PV}{GM^2/R} \propto \rho^\gamma R^4 \propto R^{4-3\gamma}$$

## Centrifugal Support and Angular Momentum Conservation

**When R decreases,  $E_{rot}/E_{grav}$  increases:**

=>(magnetic) braking process

$$j = R^2 \omega(t) = R_0^2 \omega_0$$
$$\frac{E_{rot}}{E_{grav}} = \frac{MR^2 \omega^2}{GM^2/R} \propto \frac{1}{R}$$

## Magnetic Support and Flux Conservation

**When R decreases,  $E_{mag}/E_{grav}$  is constant:**

Typically one infers  $\mu = (M/\phi)/(M/\phi)_c = 1-4$   
(Crutcher et al. 1999, 2004)

$$\phi \propto BR^2$$
$$\frac{E_{mag}}{E_{grav}} = \frac{B^2 R^3}{M^2/R} \propto (\phi/M)^2$$

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# The Issue of Radiative Pressure

The coupling occurs through the coupling of the radiation to the dust  
=> Treating well the radiative transfer and the micro-physics

Larson & Starrfield 1971 (Kahn 1974) :

+ Collapse conditions =>

$$\text{Radiation Pressure} / \text{Dynamical Pressure} = 1 \quad \Rightarrow \quad \frac{L/4\pi r^2 c}{\rho u^2} \approx 1$$

+  $u^2 = 2GM/r \Rightarrow \frac{L/4\pi r^2 c}{\rho u^2} \approx 1.3 \times 10^{-11} \frac{L/L_S}{(M/M_S)^{1/2}} r^{1/2}$

+ the radius where grains vaporize corresponds to => T=1500 K

+ Estimate of T using simple radiative transfer

=>Radiative Pressure / Dynamical Pressure =  $2 \times 10^{-5} \frac{(L/L_S)^{6/5}}{(M/M_S)^{3/5}}$

**leads to  $M \sim 20 M_S$**

Wolfire and Cassinelli (1985):

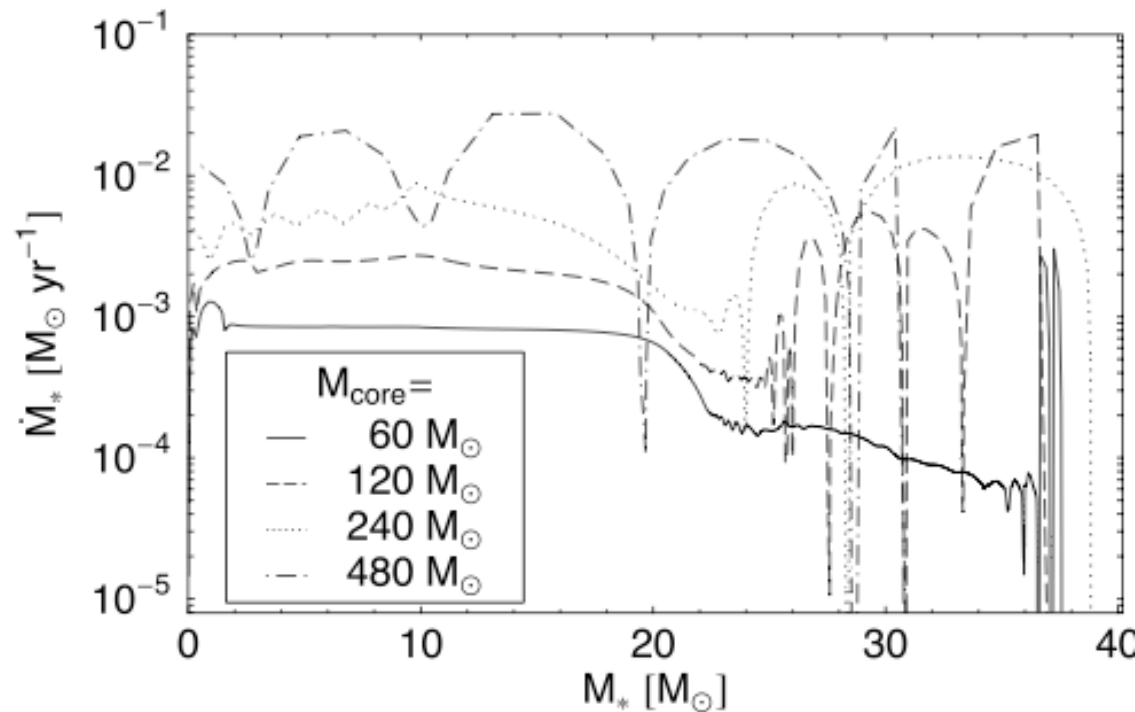
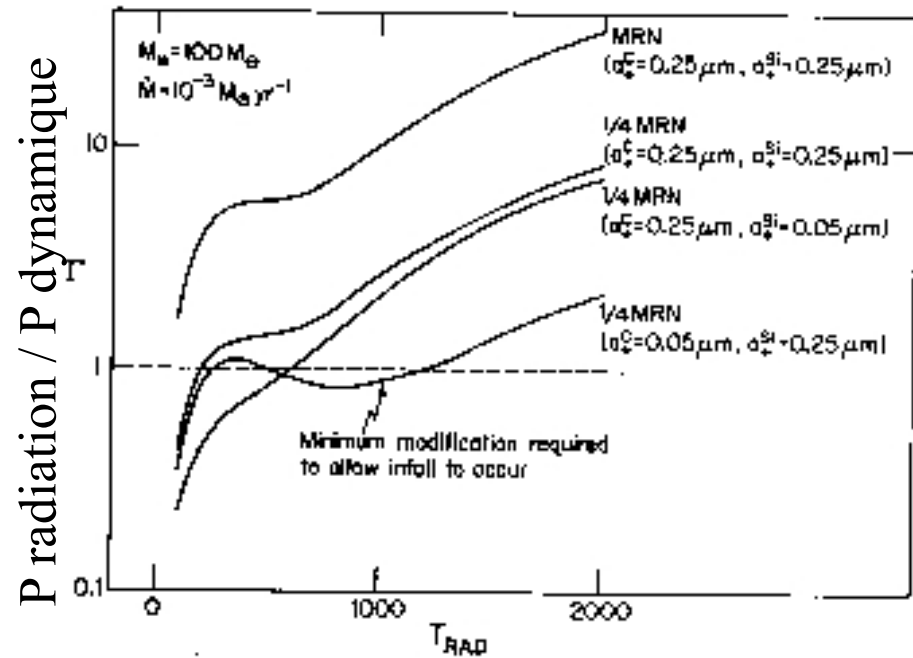
-assume a constant accretion rate of  $10^{-3} M_{\odot}/\text{an}$

-consider a classical (Matthis et al. 1977) grains distribution

-explore the influence of a grain deficit

A 100  $M_{\odot}$  stars cannot form with a standard grain abundance (1/4 is required)

**Solution:**  
**weak abundance of grains**



1D results by Kuiper et al. (2010)

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# The Multi-D approach

(e.g. Yorke & Sonnhalter 2002, Krumholz et al. 2009, Kuiper et al. 2010)

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

$$\frac{\partial (\rho \mathbf{v})}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) = -\nabla P - \rho \nabla \phi,$$

$$\frac{\partial (\rho e)}{\partial t} + \nabla \cdot [(\rho e + P) \mathbf{v}] = \rho \mathbf{v} \nabla \phi - \kappa_R \rho (4\pi B - cE),$$

$$\nabla^2 \phi = 4\pi G \left[ \rho + \sum_n m_n \delta(\mathbf{x} - \mathbf{x}_n) \right],$$

$$\frac{\partial E}{\partial t} - \nabla \cdot \left( \frac{c\lambda}{\kappa_R \rho} \nabla E \right) = \kappa_P \rho (4\pi B - cE) + \sum_n L_n W(\mathbf{x} - \mathbf{x}_n)$$

$$L_n = \frac{G\dot{M}M}{R} + L_*$$

$$\kappa_R = 0.1 + 4.4(T_g/350) \text{ cm}^2 \text{ g}^{-1},$$

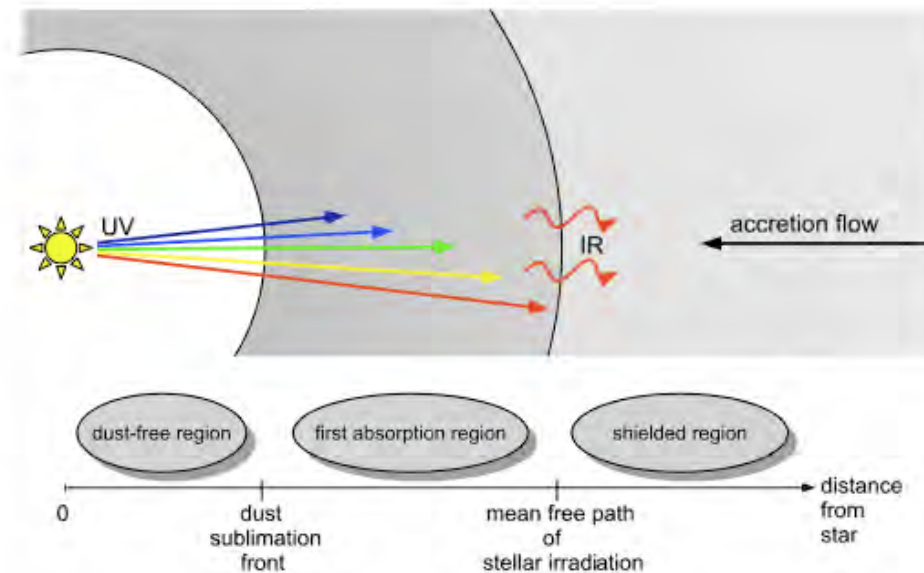
$$\kappa_P = 0.3 + 7.0(T_g/375) \text{ cm}^2 \text{ g}^{-1}.$$

Flux limited diffusion method:

-implicit methods : expensive

-usually assume grey-body except Yorke & Sonnhalter who do multi-frequency

-Kuiper et al. use an hybrid scheme, treating FLD as grey but also include the direct illumination from central stars (multi-wavelength)





2D results by Yorke & Sonnhalter (2002)

Solution of the radiative pressure problem:  
the anisotropy due to the disk, *The flashlight effect*  
(Yorke & Bodenheimer 99)

-due to centrifugal force, matter piles up in the equatorial plan

-bigger optical depth in the equatorial plan than along the pole

-the photons escape in this direction and the radiative pressure is reduced

Yorke & Sonnhalter  
(2D, 64 wavelengths)

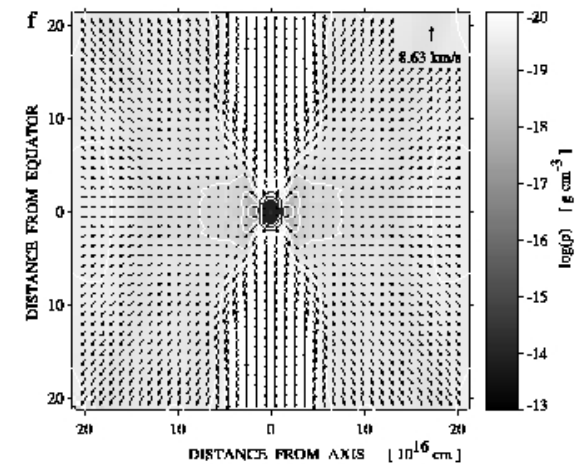
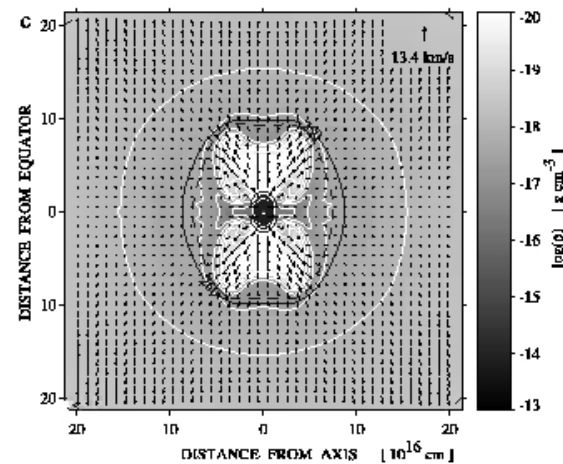
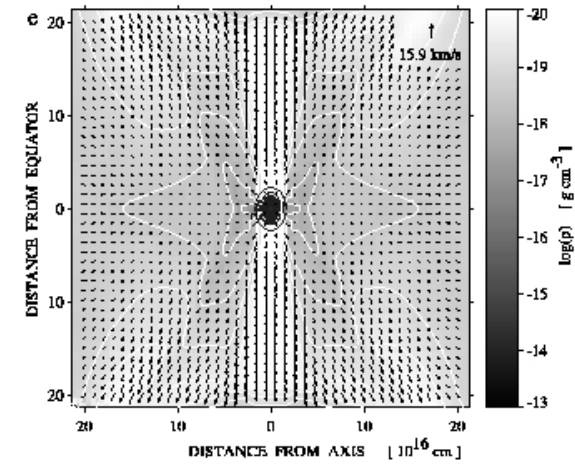
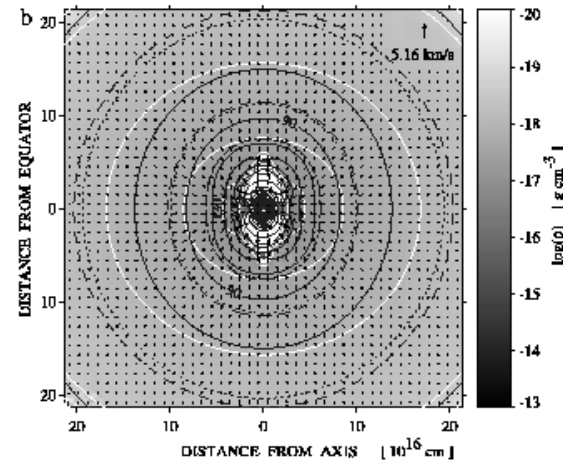
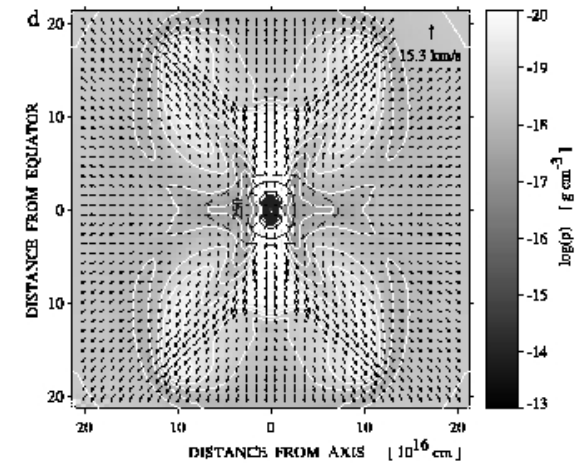
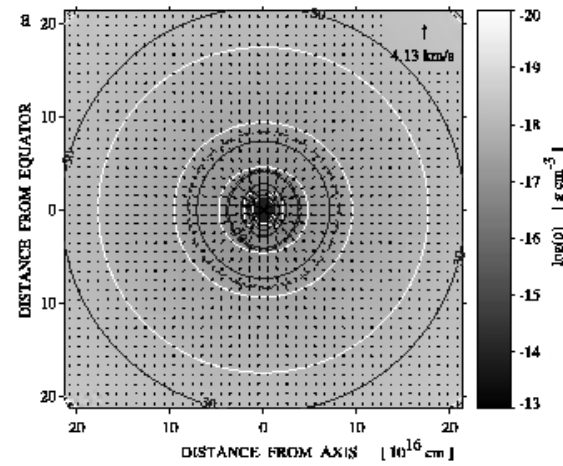
+collapse nearly spherical

+flattening in the equatorial plan

+formation of outflows along the pole

+eventually expansion even along the equatorial plan

Formation of 33 Ms star  
(total mass 60).



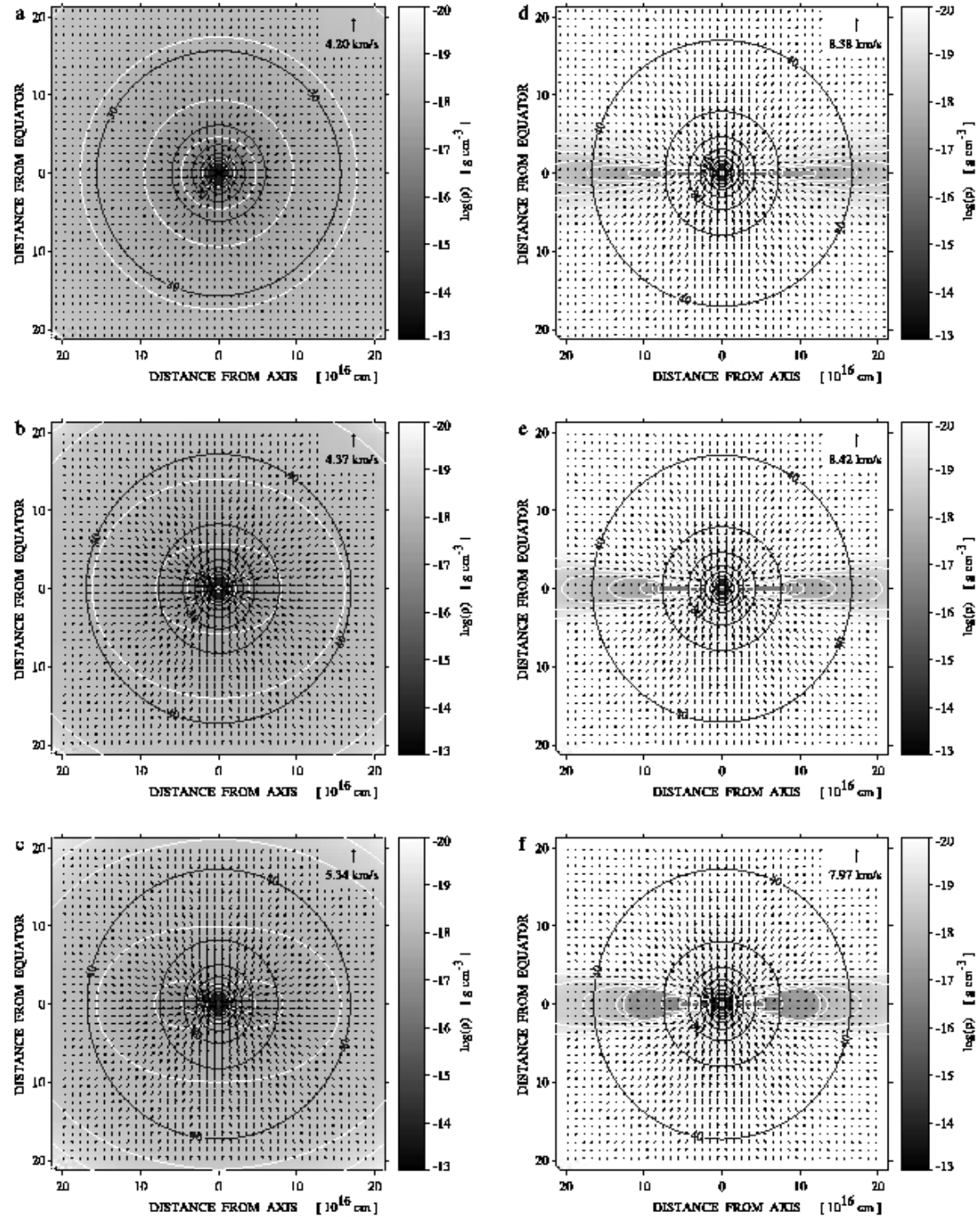
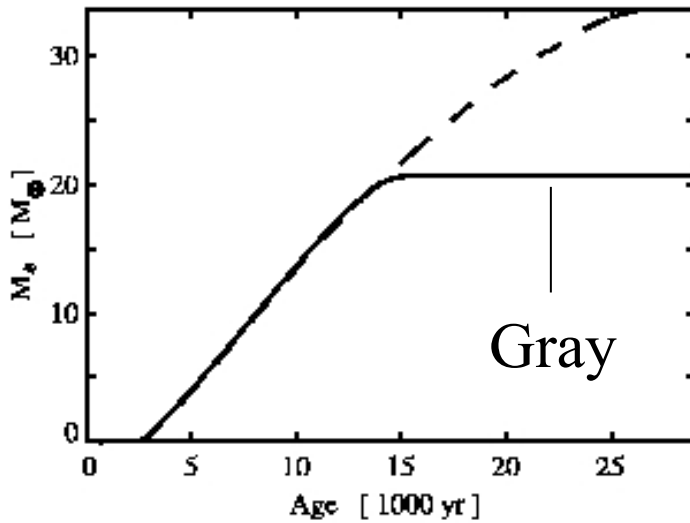
Yorke & Sonnhalter

Identical but grey treatment

Important differences :

-no outflow

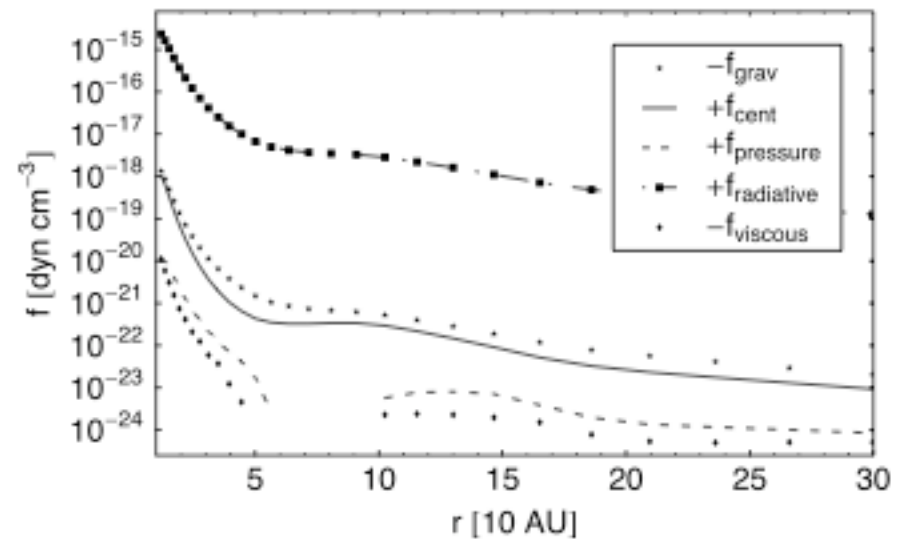
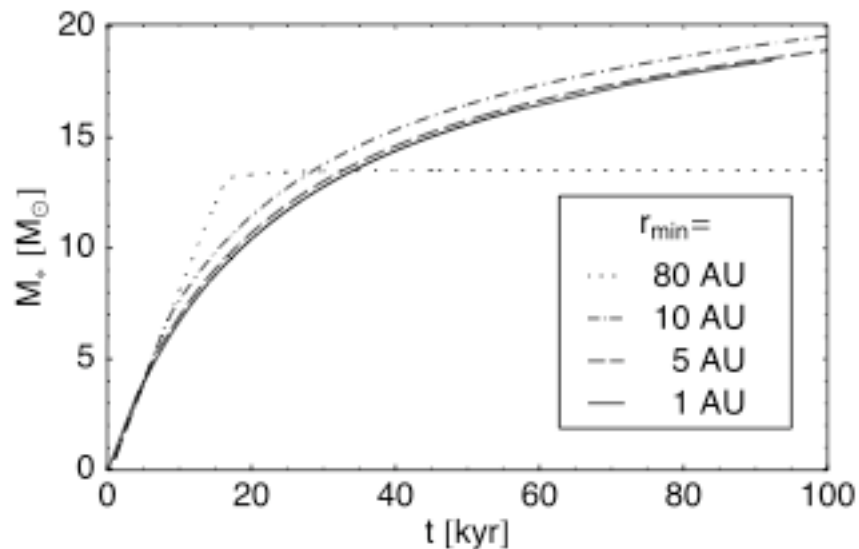
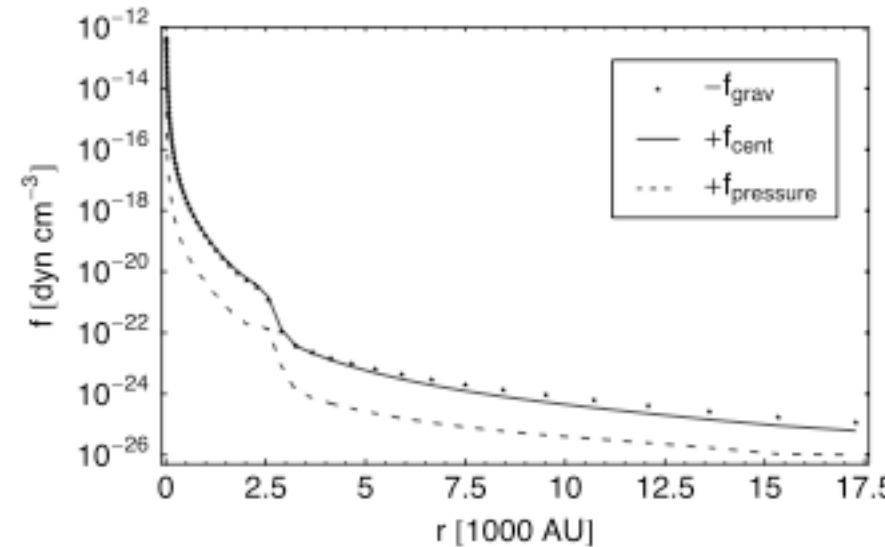
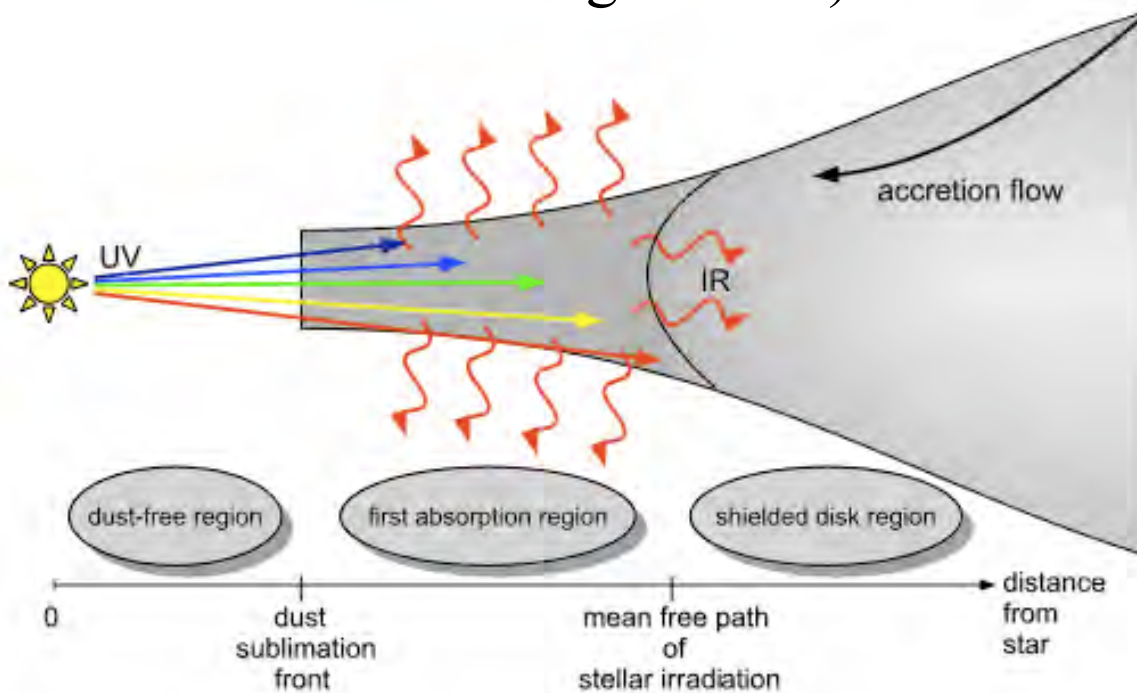
-Final Mass : 20  $M_{\odot}$   
(total mass 60  $M_{\odot}$ ).



# Results of Kuiper et al. 2010

## Importance of solving the dust free regions

(otherwise the radiation is too isotropic and this stops the Flashlight effect)



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-magnetized non-radiative

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-Where the gas is coming from ?

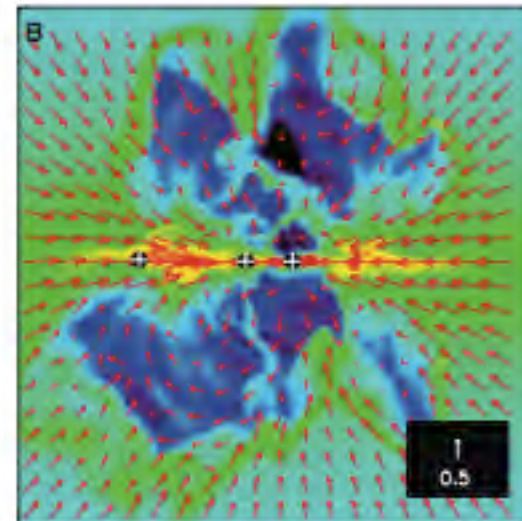
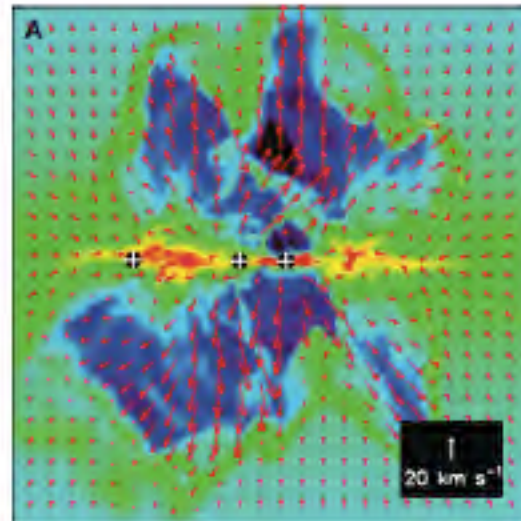
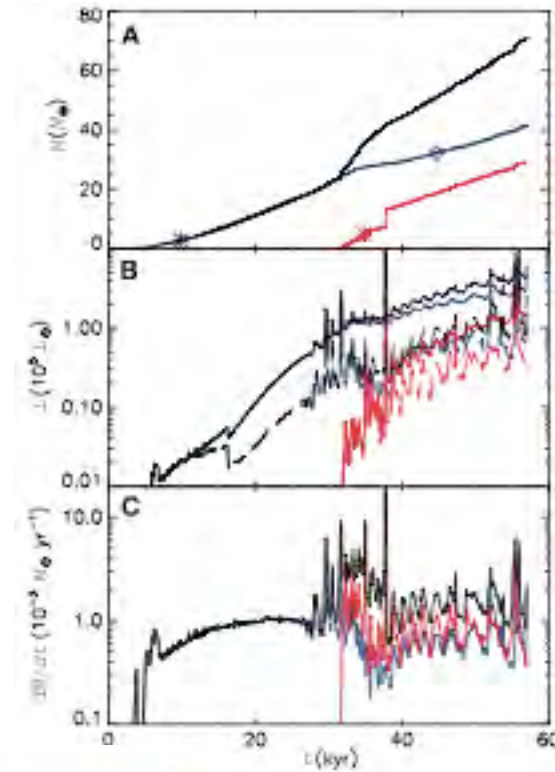
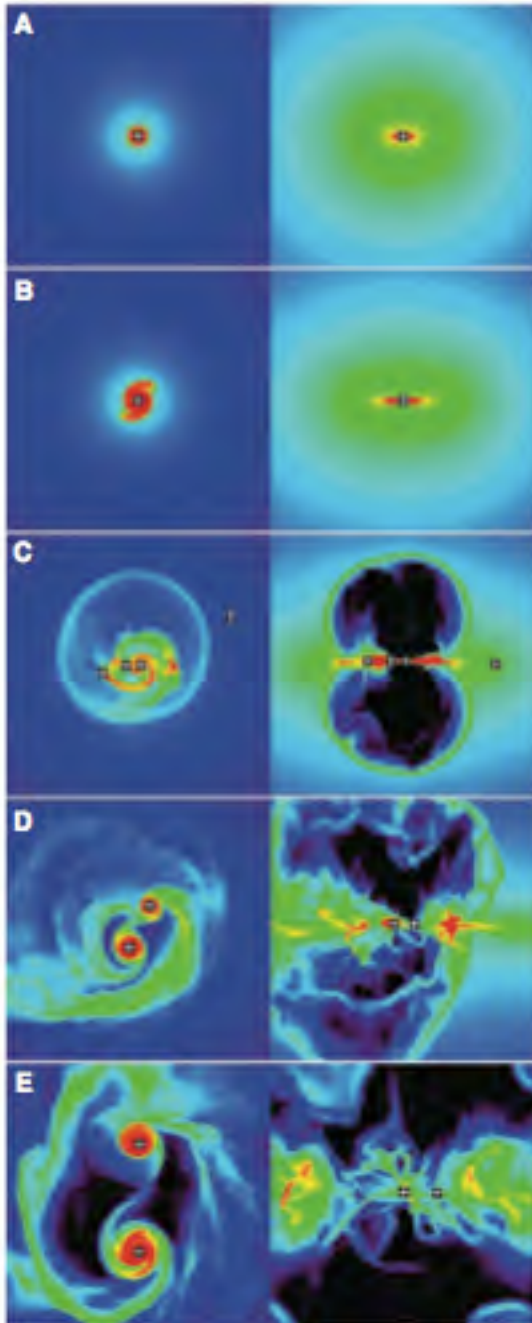
-competitive accretion

-gravitational well based theory

-tracing the gas in simulations

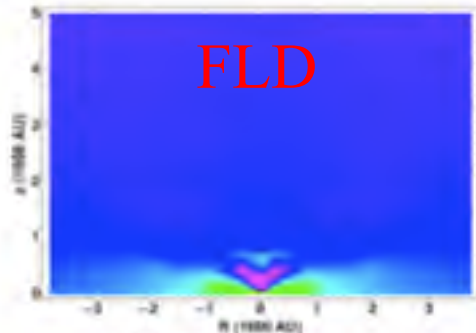
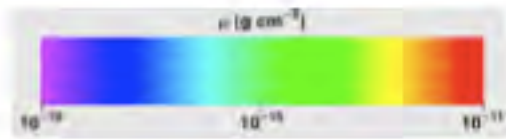
3D results by Krumholz et al. 2009

The cavity becomes unstable to Rayleigh-Taylor instability and more gas is accreted

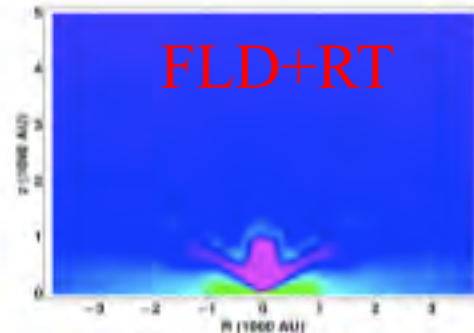


# Results of Kuiper et al. 2011

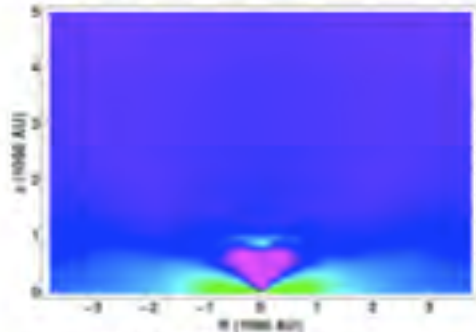
The instability of the cavity is due to the FLD scheme  
The hybrid scheme (FLD+ray tracing) leads to higher radiative pressure and no instability



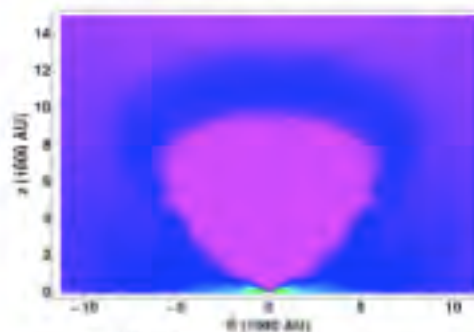
(a) FLD run at  $t = 44$  kyr



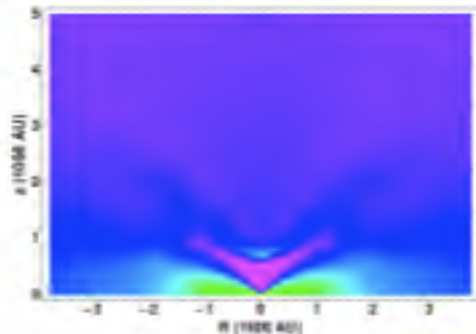
(b) RT+FLD run at  $t = 39$  kyr



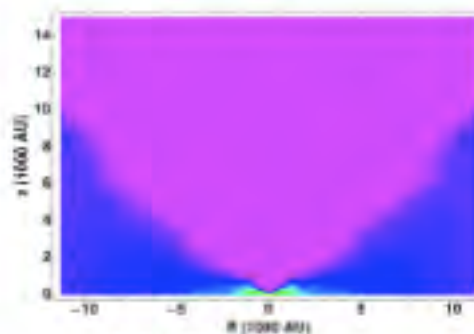
(c) FLD run at  $t = 49$  kyr



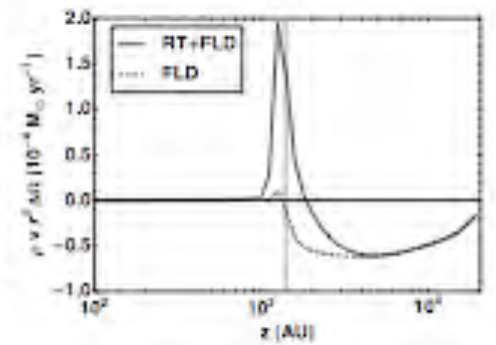
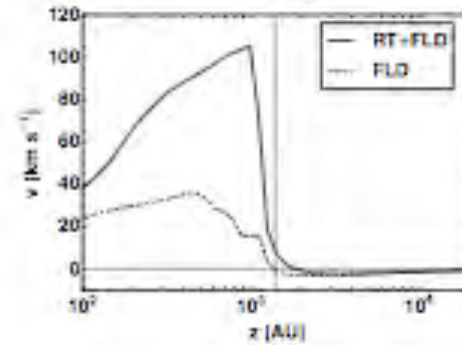
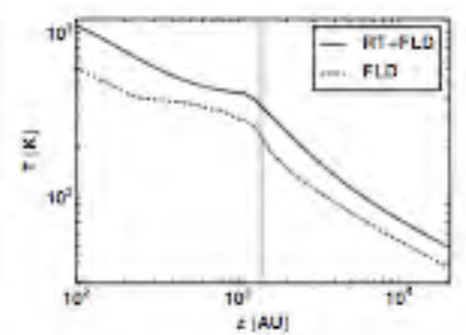
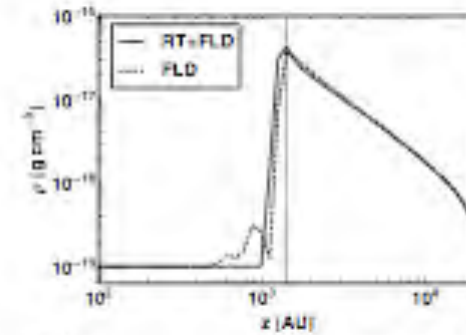
(d) RT+FLD run at  $t = 44$  kyr



(e) FLD run at  $t = 52$  kyr



(f) RT+FLD run at  $t = 42$  kyr



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-1D : grain solution

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**-collision model**

-Can we prevent the gas to fragment in many objects ?

-isothermal

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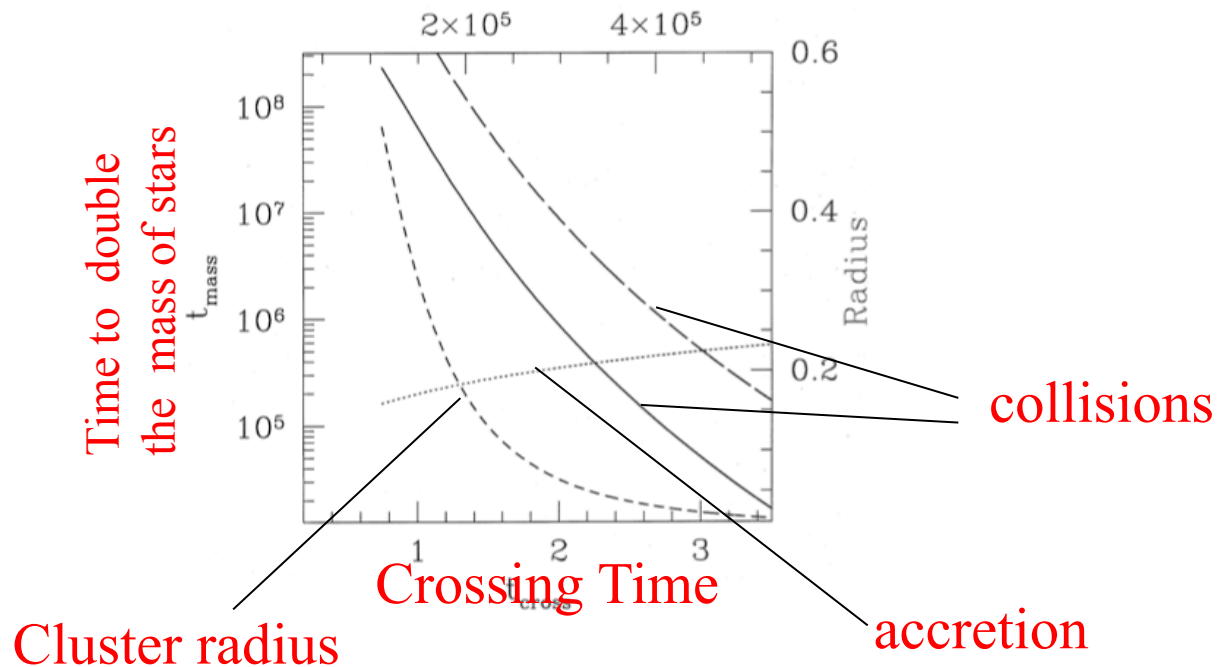
# The collision model

Alternative Scenario (Bonnell et al. 98, 02, 04):

**Formation of massive stars by « merging » of low mass stars**

**The radiative pressure has no influence on the collisions between stars**

Bonnell et al. 98 develop a Toy model that takes into account accretion, merging by collision and cluster dynamics.



=> efficiency required  
 $10^8$  stars/pc<sup>2</sup>

# Estimate using direct simulations

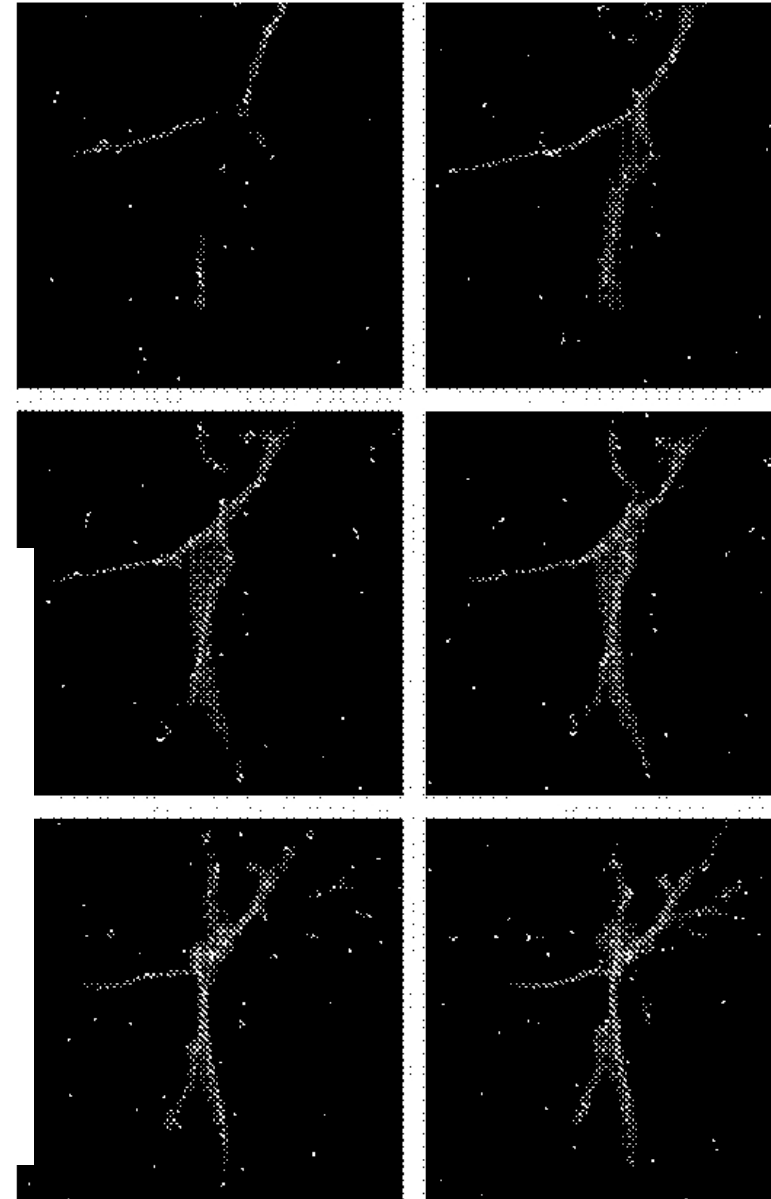
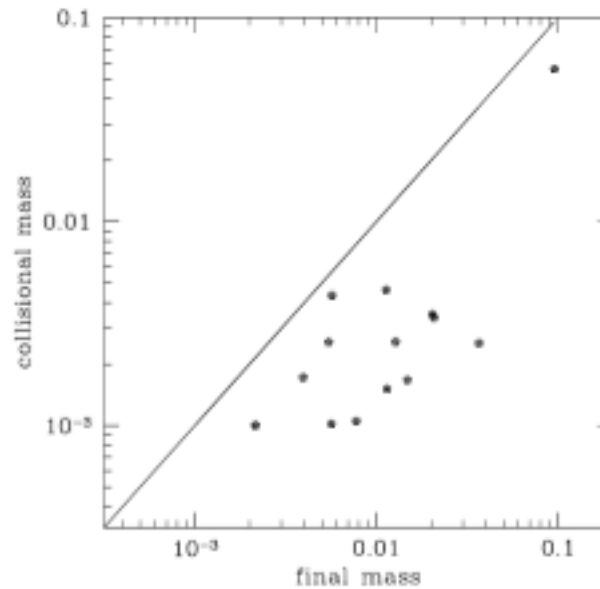
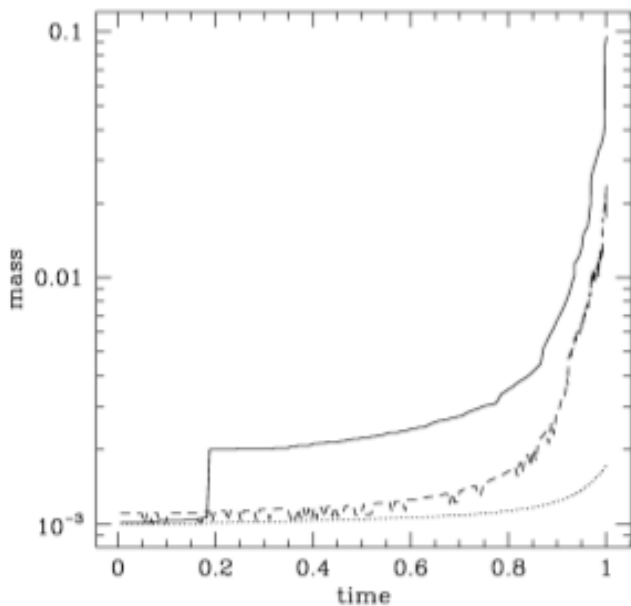
(Bonnell & Bate 02,05)

SPH with 1,000,000 of particules, use sink particles

Possible to merge the sinks (distance threshold)

- +Mass of most massive stars
- +Mean mass in the cluster core
- +Mean mass

Mass due to collisions  
as a function of the final  
mass



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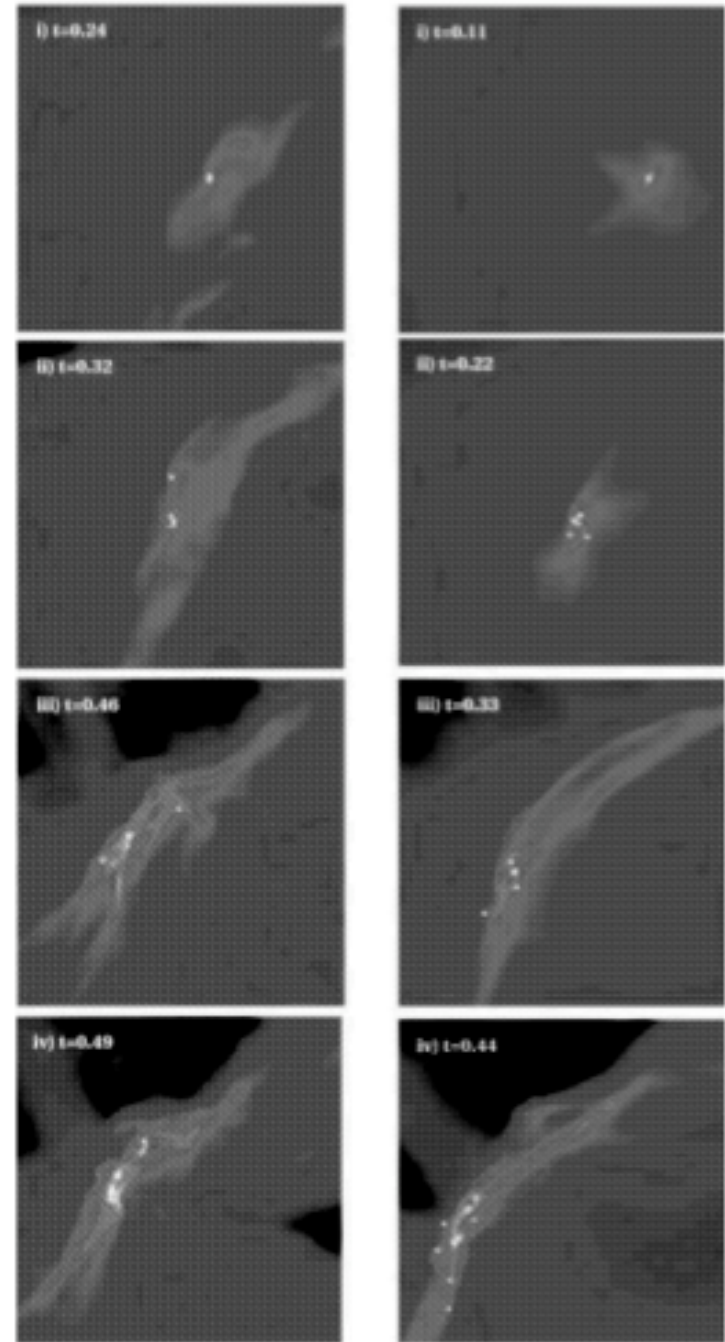
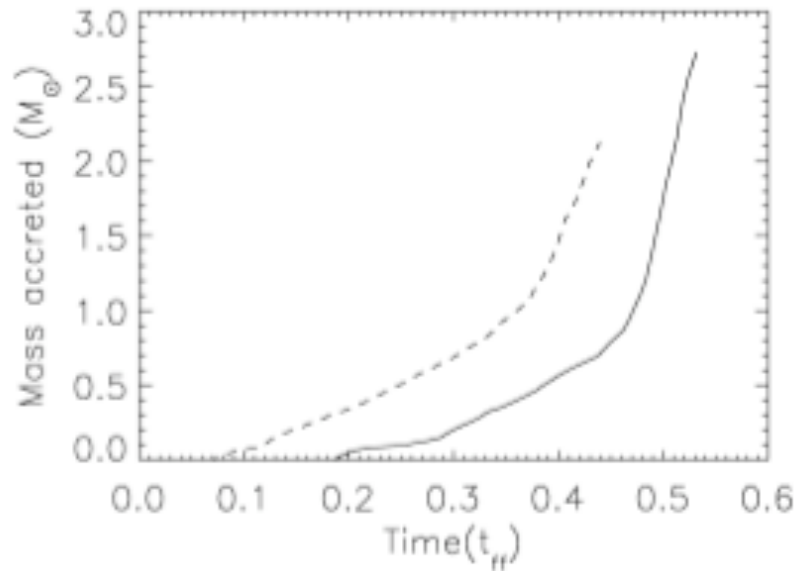
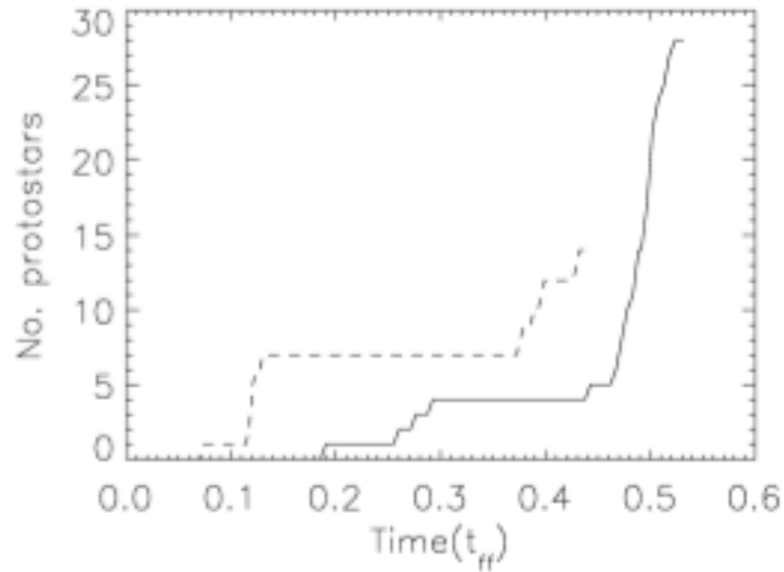
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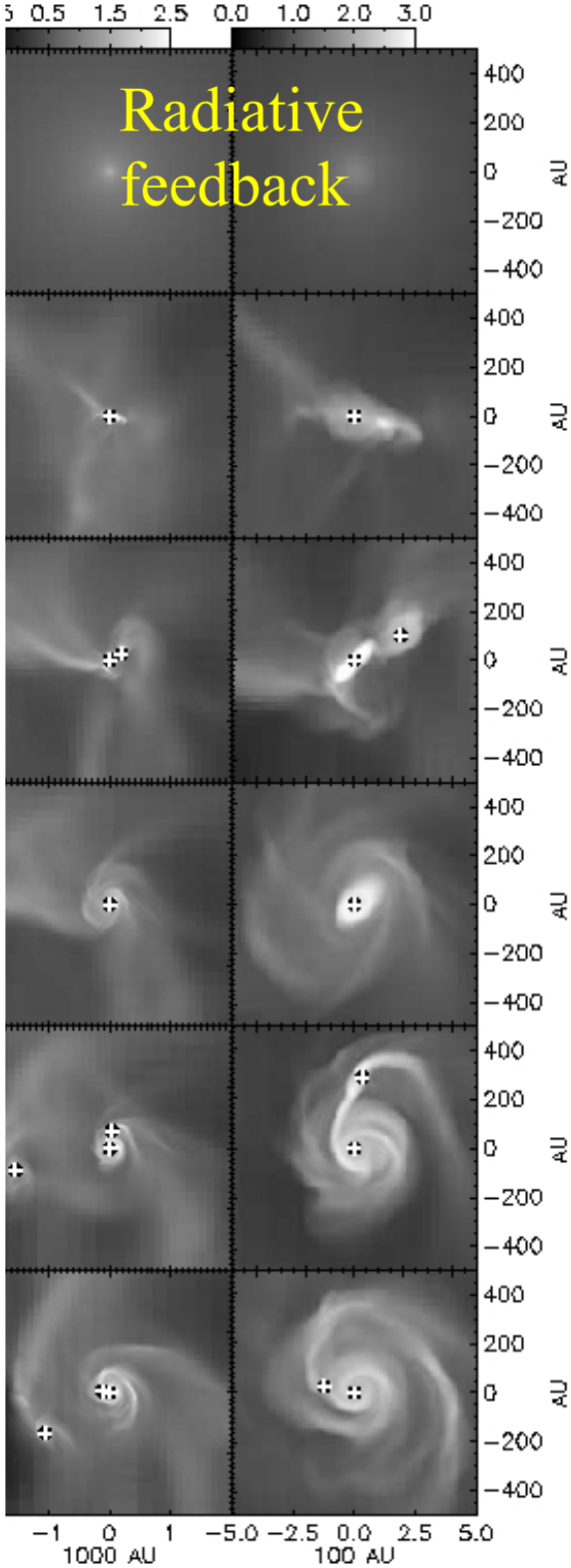
# Fragmentation of a collapsing unmagnetized isothermal Massive core (Dobbs et al. 2005)



The core fragments in many objects therefore limiting the mass of stars.

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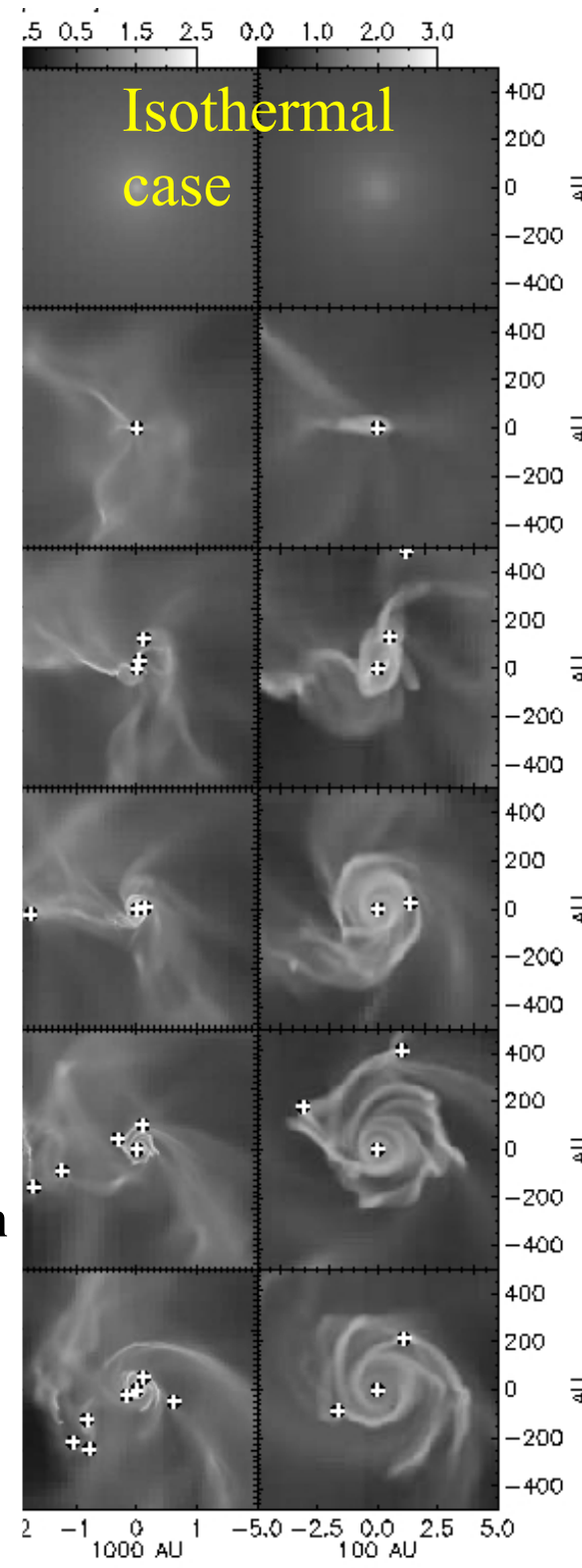


## Influence of the radiative feedback on a massive core

Krumholz et al. 2007

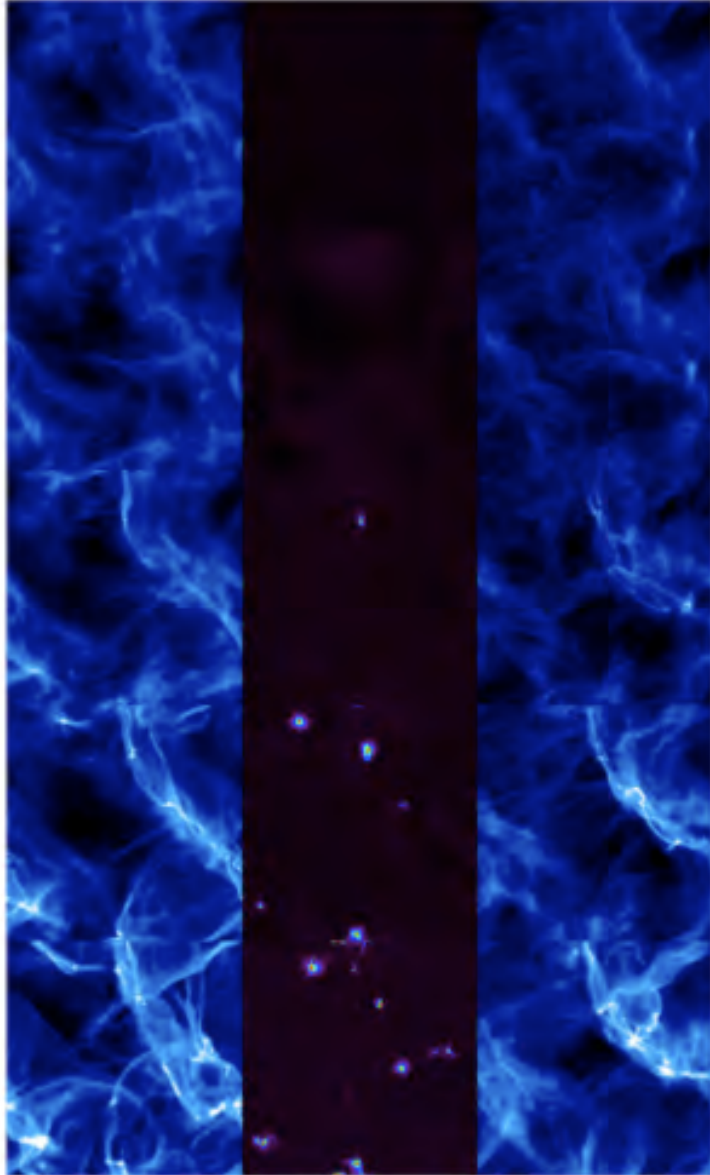
**Radiative feedback reduces the number of fragments simply because it increases the temperature and increases the Jeans mass**

**Note however that the initial conditions are very peaked (singular isothermal sphere) and tend to prevent fragmentation**  
Girichidis et al. 2010



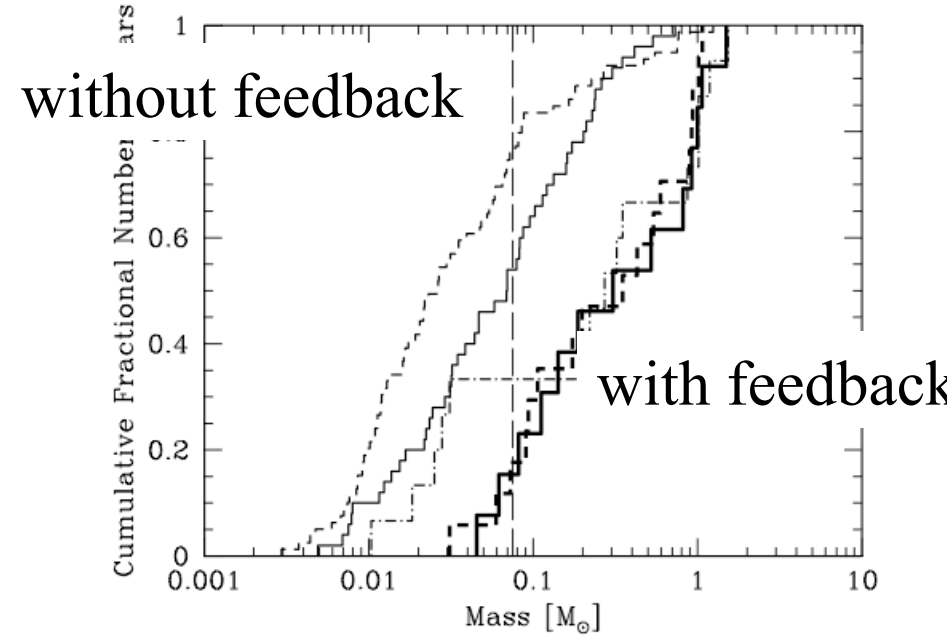
# Influence of the protostellar feedback : further calculations

Bate 2009, Offner et al. 2009, Commerçon et al. 2010, Tomida et al. 2010, Krumholz et al. 2012



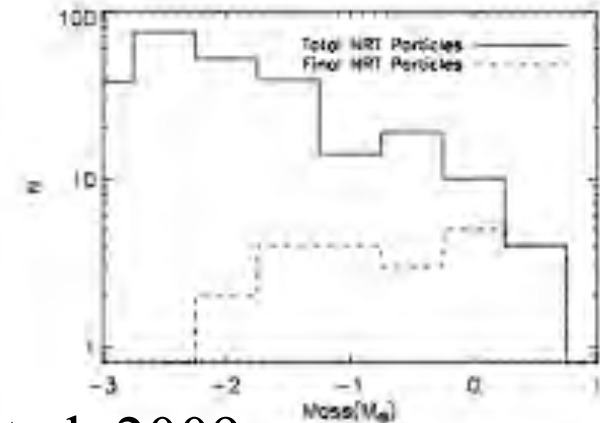
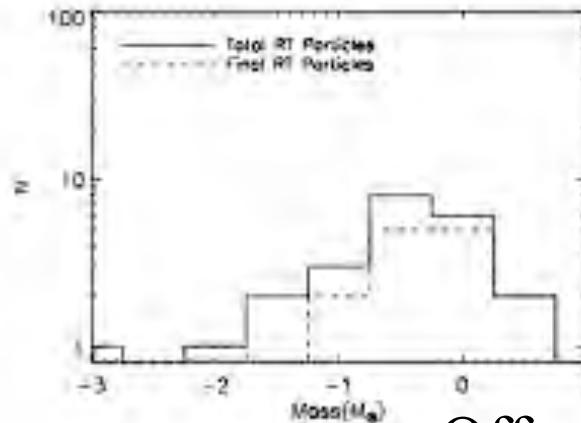
with feedback

Bate 2009, 2012



with feedback

without feedback



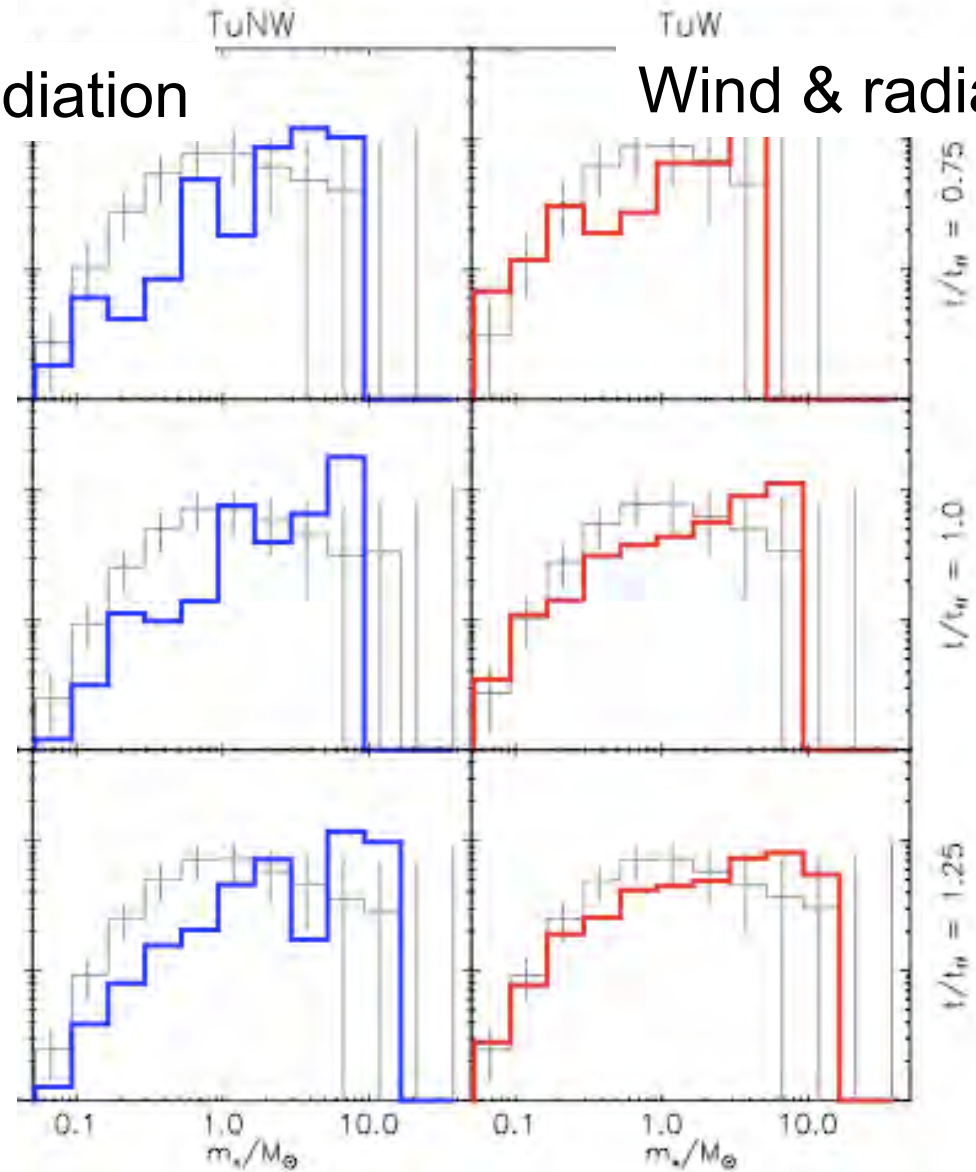
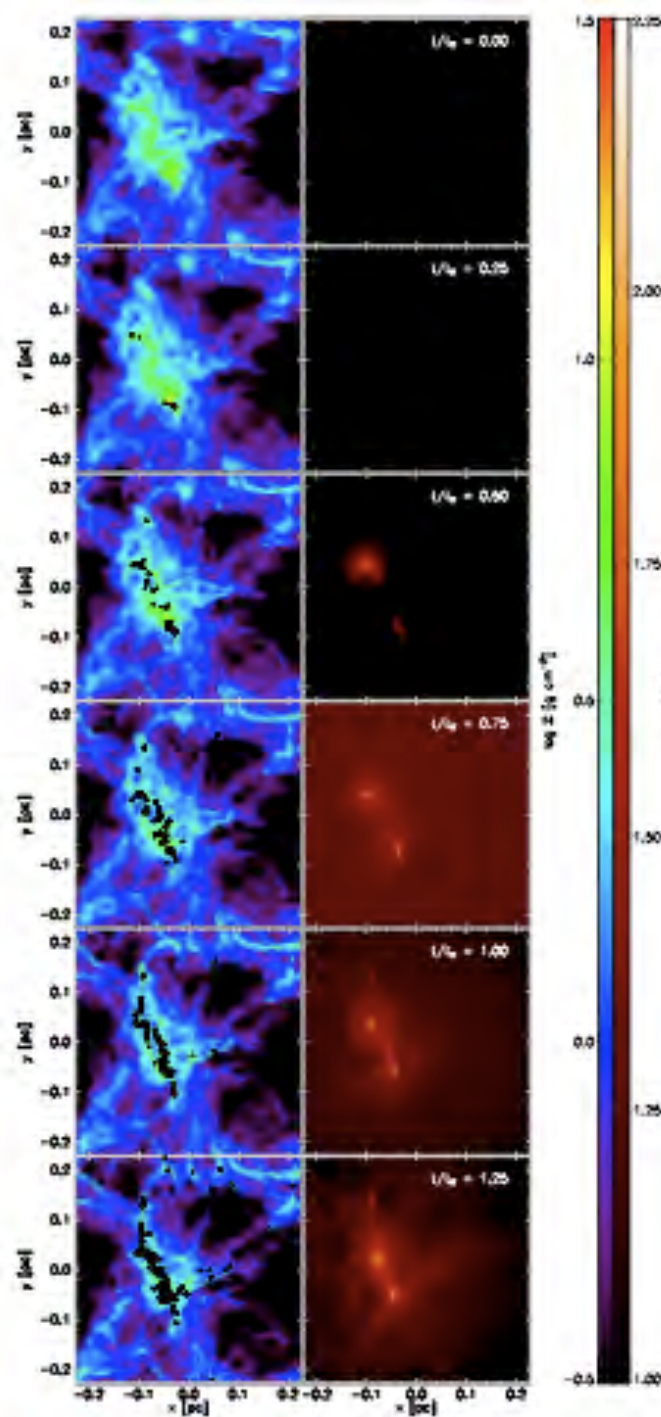
Offner et al. 2009

# Wind and Radiative feedback

Krumholz et al. 2012

Pure radiation

Wind & radiation



=> Too few low mass objects with pure radiation, winds help to reduce feedback which escape along cavities



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# Influence of a weak magnetic field on the fragmentation of low mass core

$\mu=1000$  (hydro)

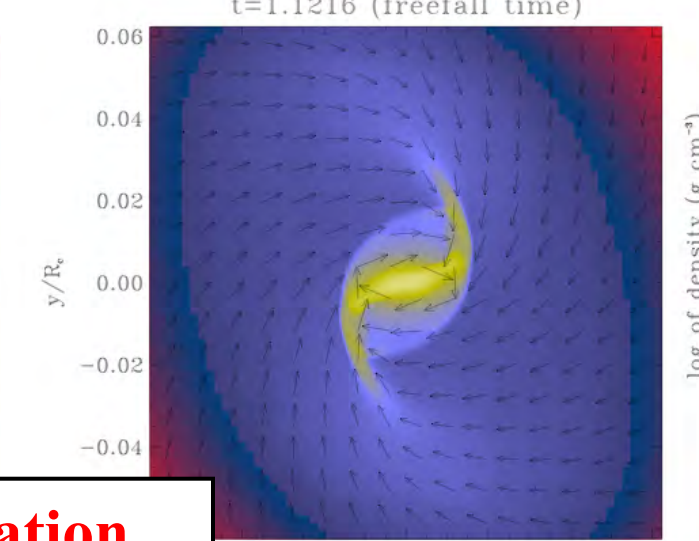
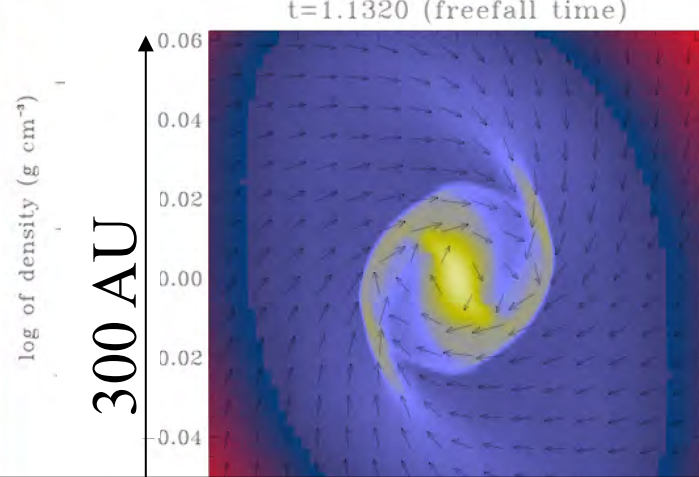
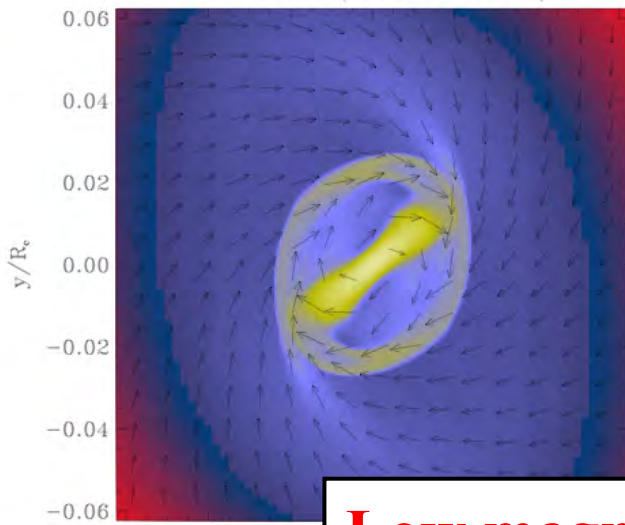
$\mu=50$

$\mu=20$

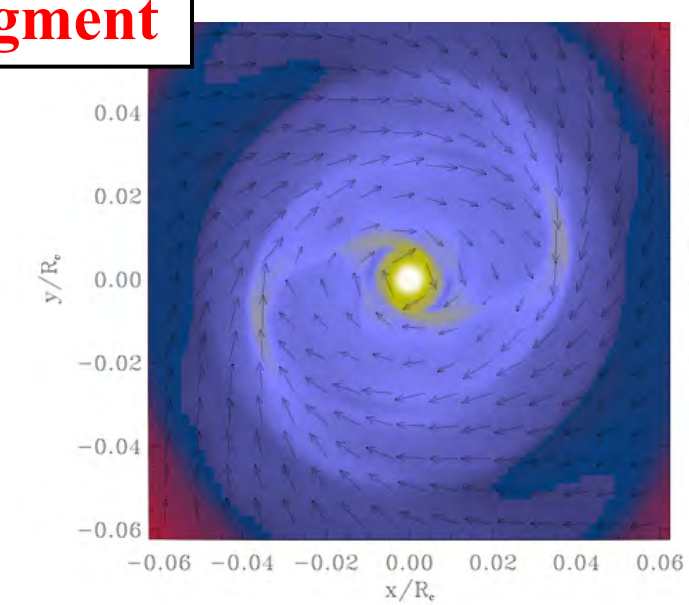
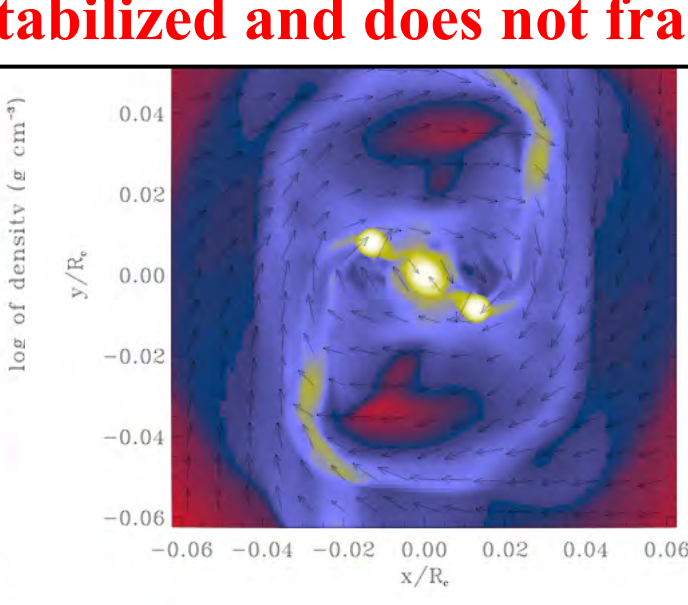
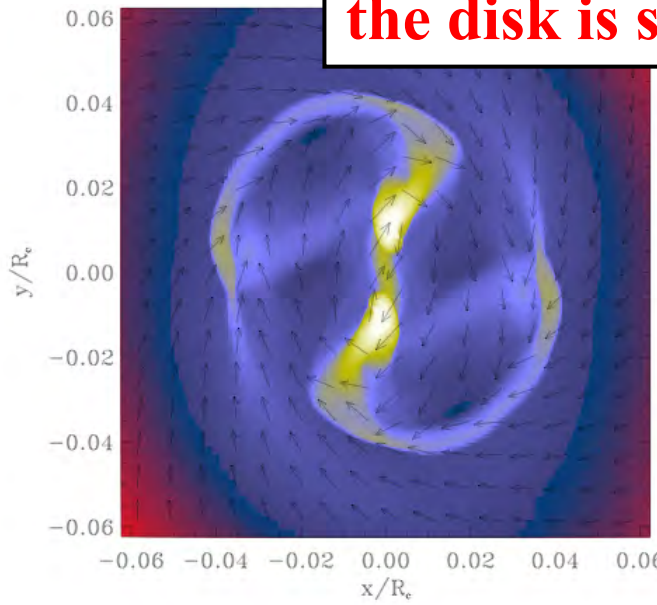
t=1.1384 (freefall time)

t=1.1320 (freefall time)

t=1.1216 (freefall time)



**Low magnetic fields allow disk formation  
but  
the disk is stabilized and does not fragment**



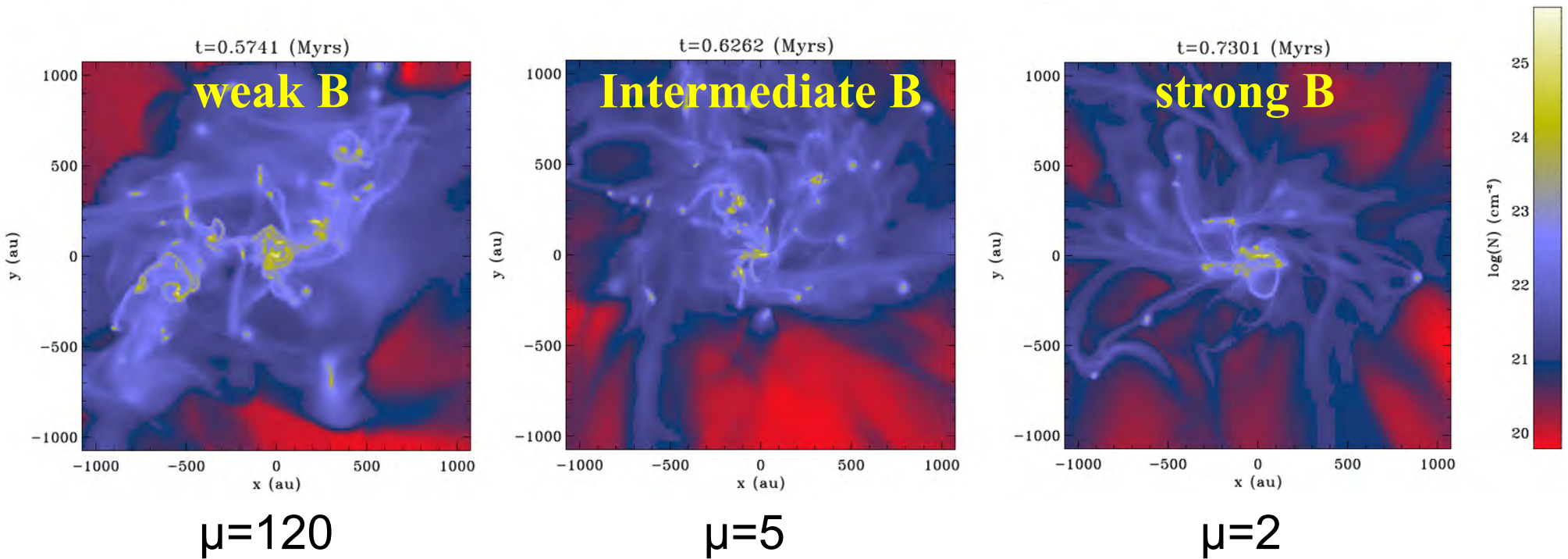
H & Teyssier 2008 (see also Machida et al. 2005)

# 100 M<sub>⊙</sub> magnetized, turbulent and dense barotropic core

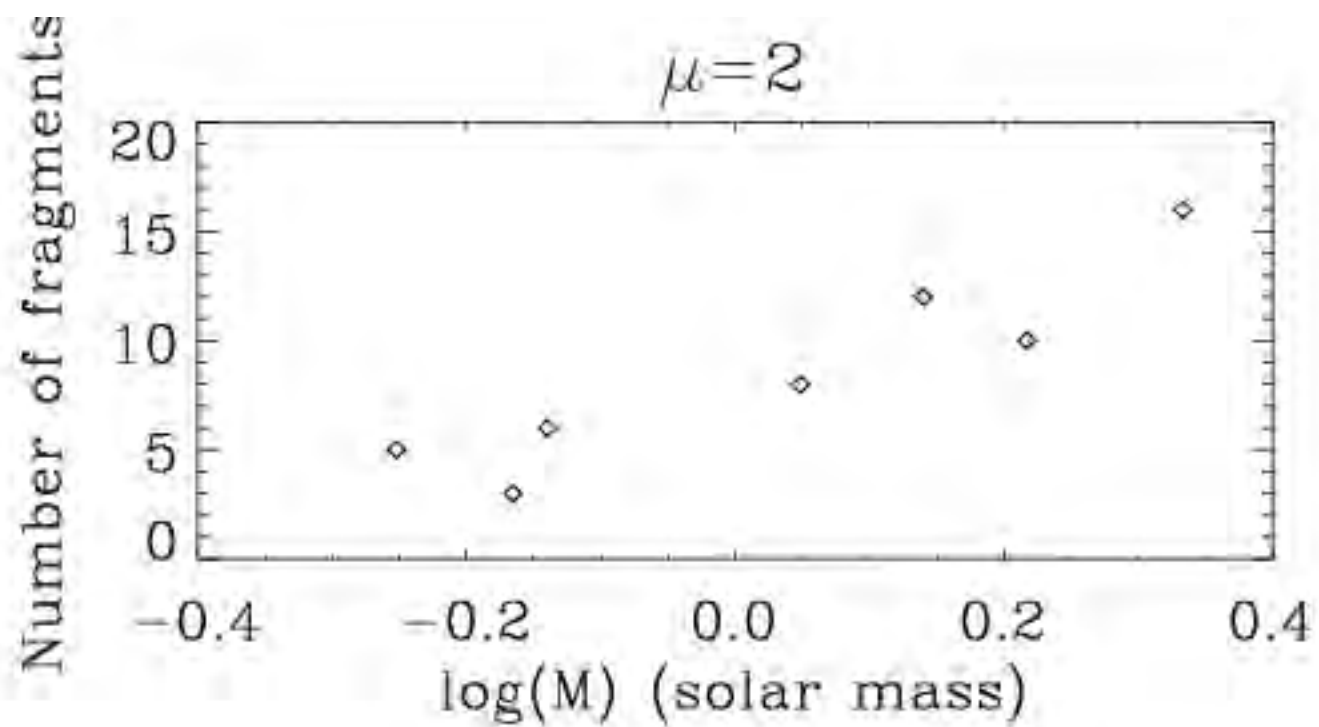
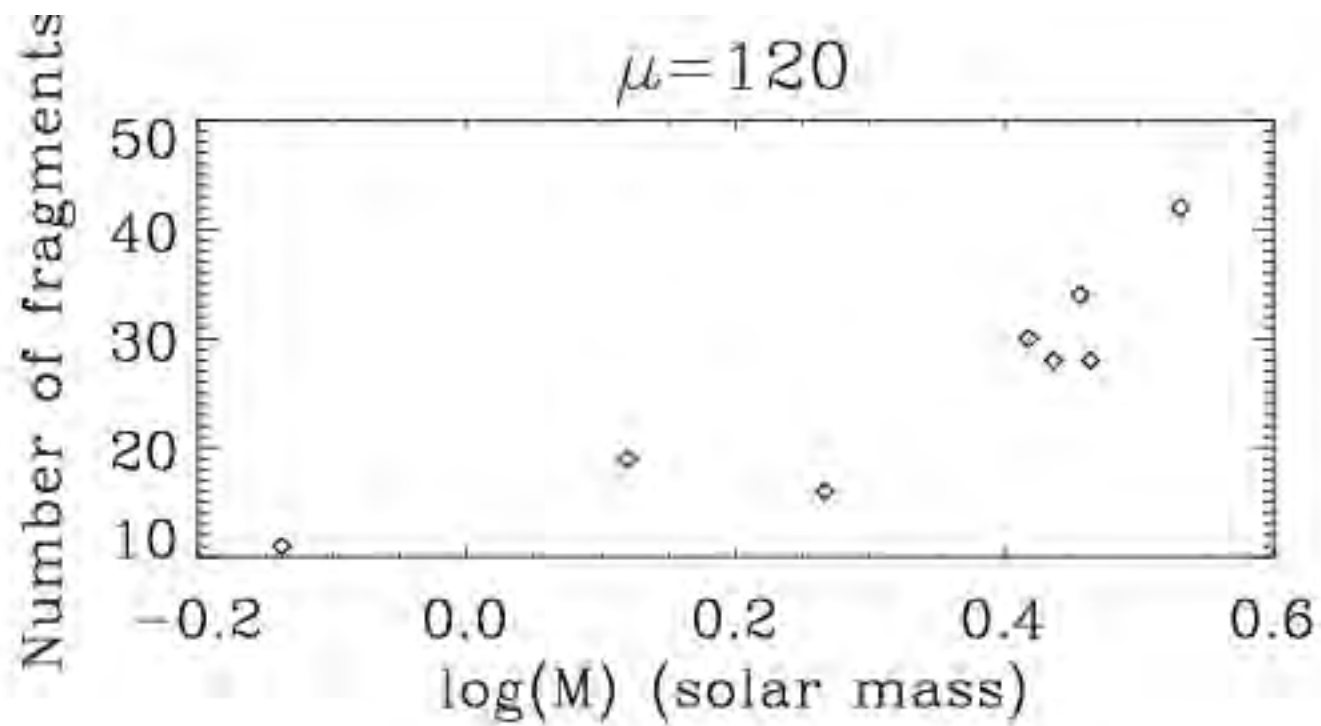
(other related works : Peters et al. 2010, Seifried et al. 2012)

Turbulence is initially seeded.  $E_{\text{turb}}/E_{\text{grav}} \sim 20\%$

In the case of a massive turbulent core, magnetic field reduces, though, do not suppress fragmentation



H+2011

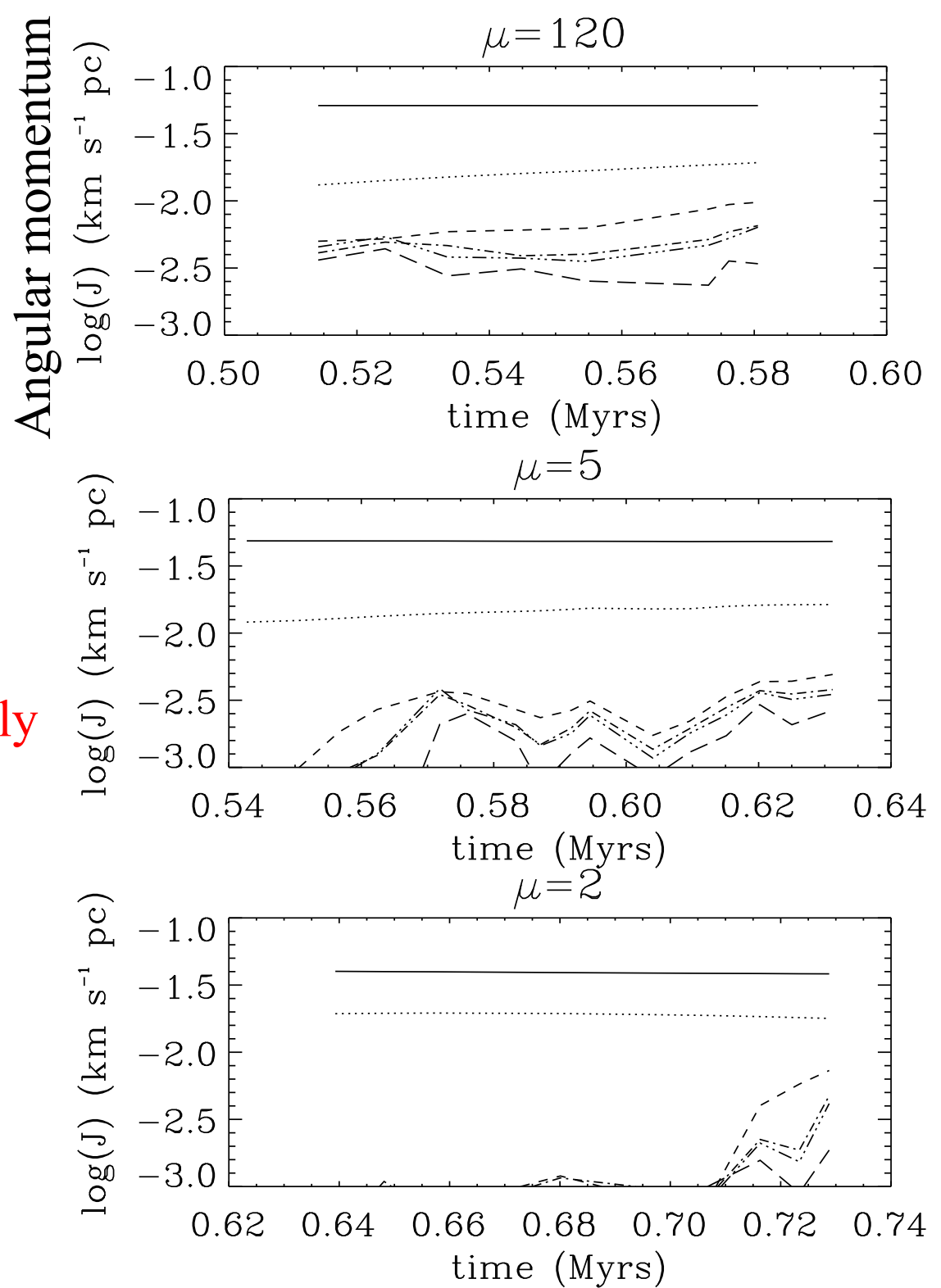


Impact of the magnetic braking:

J is much reduced as B  
Increases

=>

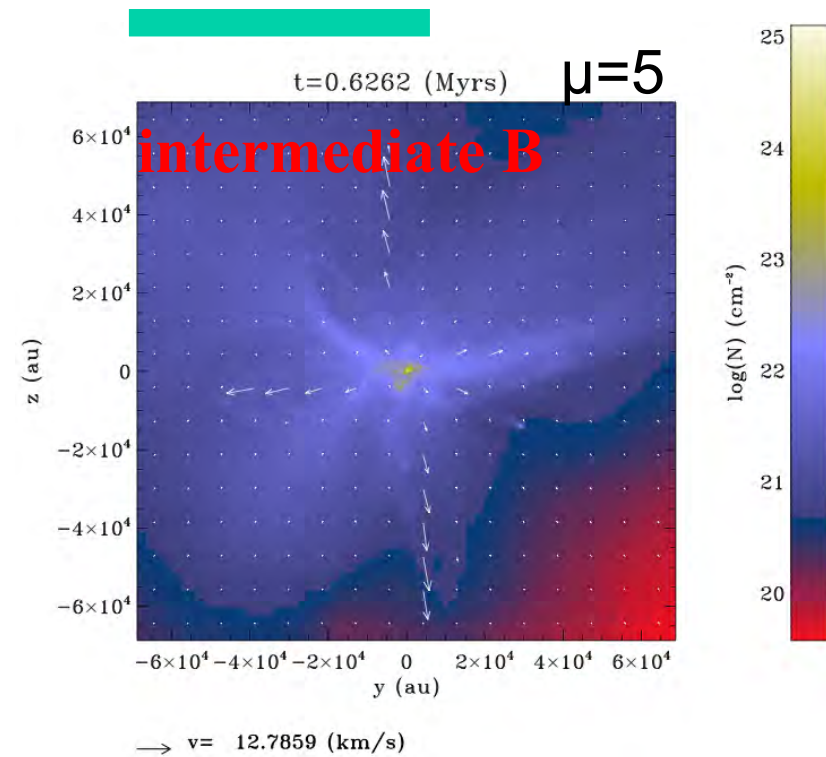
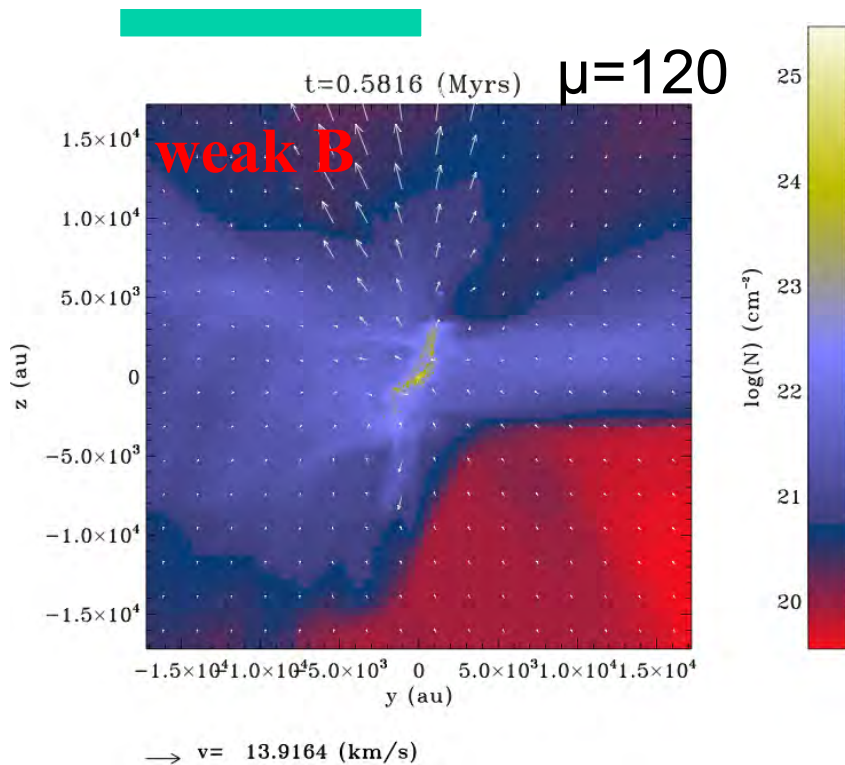
Magnetic braking is important  
even when the flow is significantly  
turbulent



# 100 M<sub>⊙</sub> magnetized, turbulent and dense barotropic core

Powerful outflows are launched even in turbulent cores

Faster flows appear with weaker fields



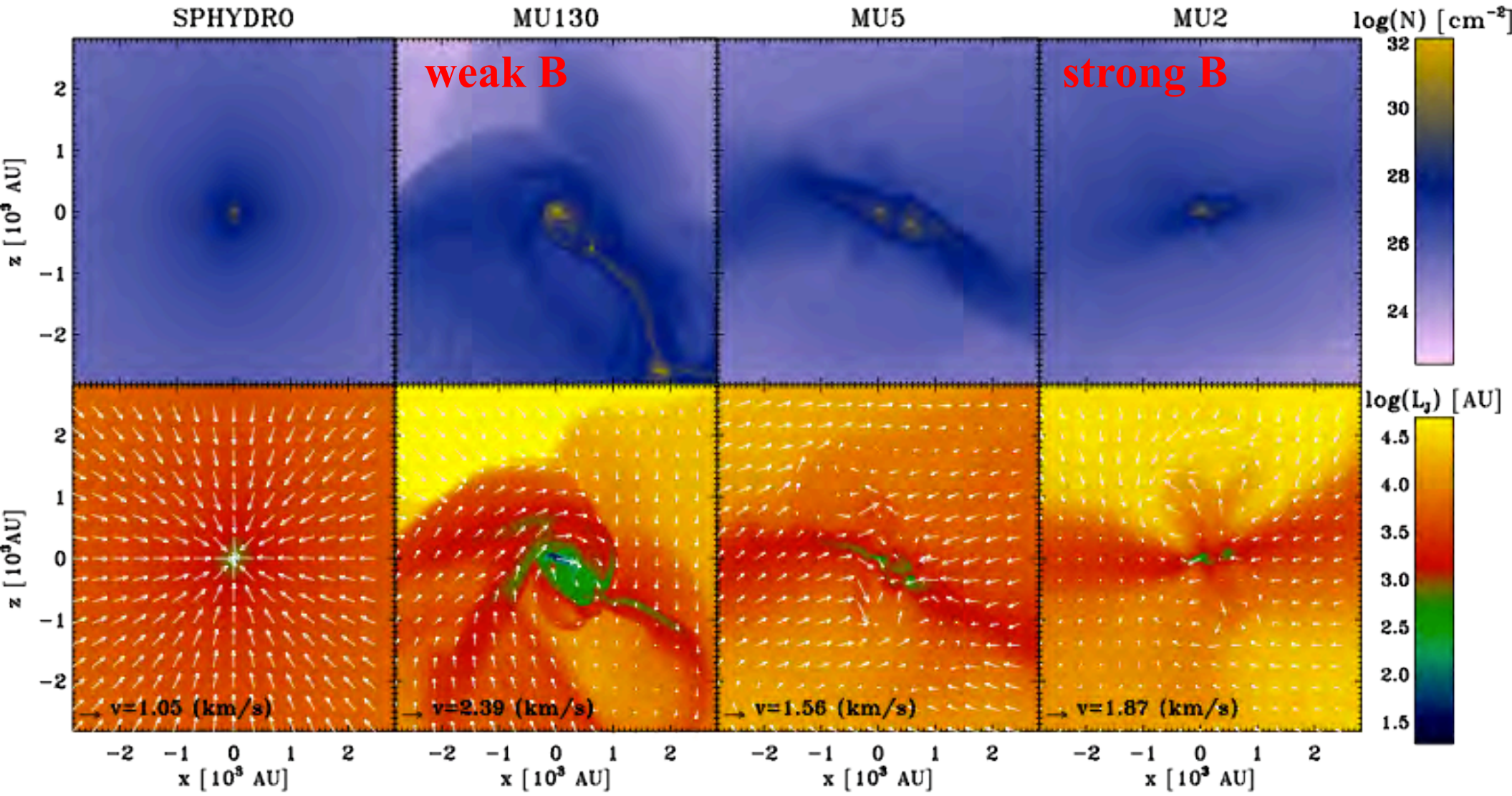
H et al. 2011

# How massive stars form ?

- Can we form massive stars in spite of the radiative pressure ?
  - 1D : grain solution
  - 2D : flashlight solution
  - 3D : radiative instability solution
  - collision model
- Can we prevent the gas to fragment in many objects ?
  - isothermal
  - radiative feedback
  - magnetized non-radiative
  - radiative and magnetized**
- Where the gas is coming from ?
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# 100 M<sub>⊙</sub> turbulent dense core collapse

$E_{\text{turb}}/E_{\text{grav}}=20\%$  initially

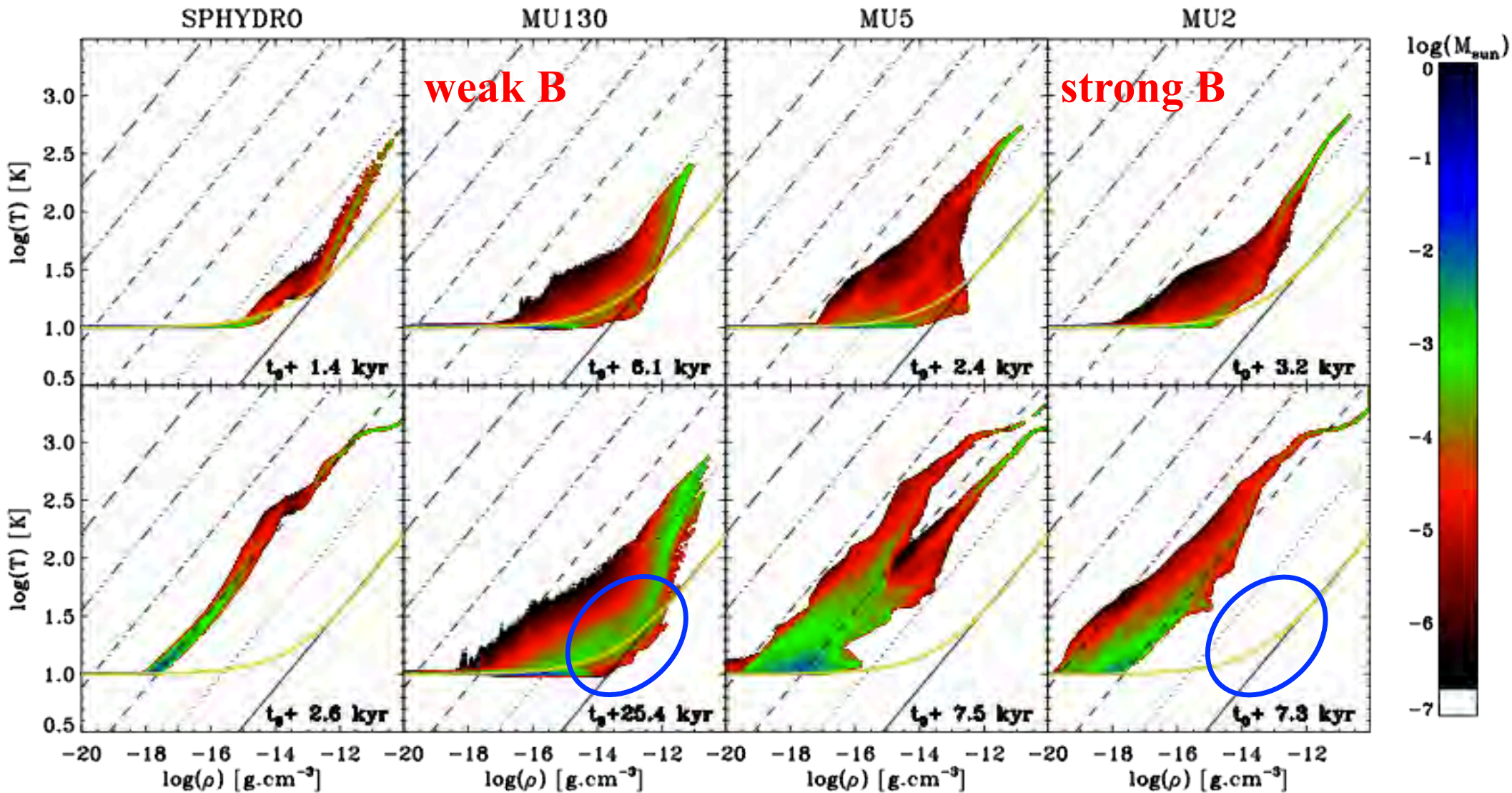


*Commerçon, H & Henning, ApJL 2011*

(see also Price & Bate 2009 at larger scales, Myers et al. 2013, 2014)

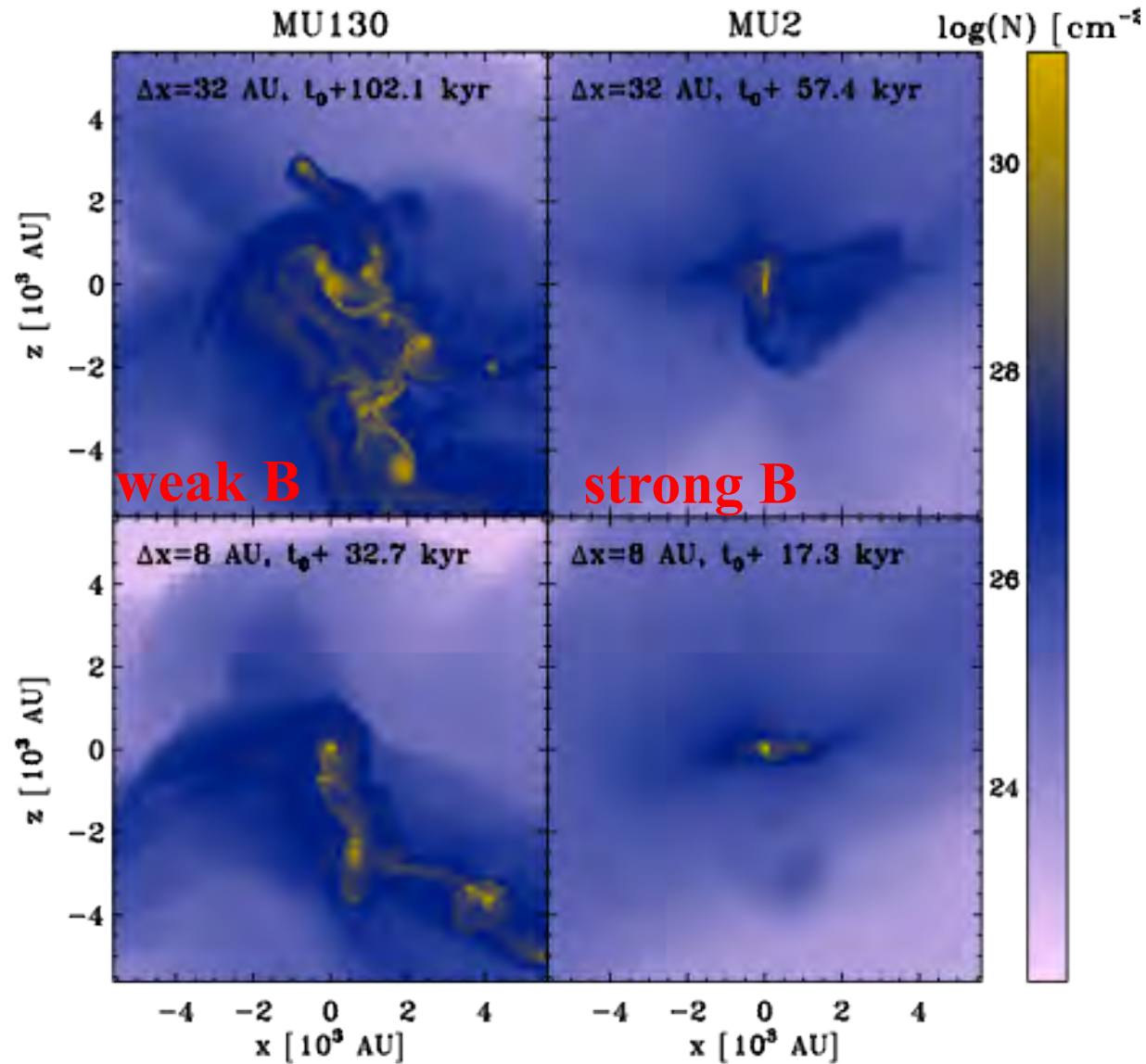


# 100 M<sub>⊙</sub> turbulent dense core collapse



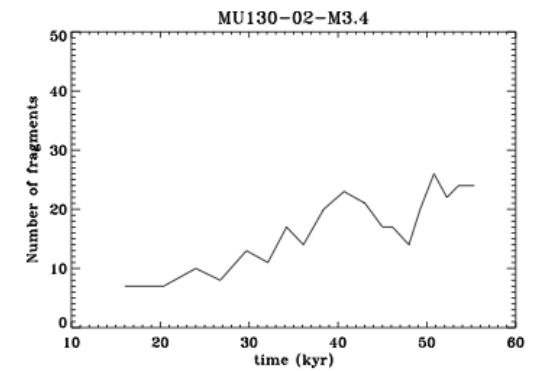
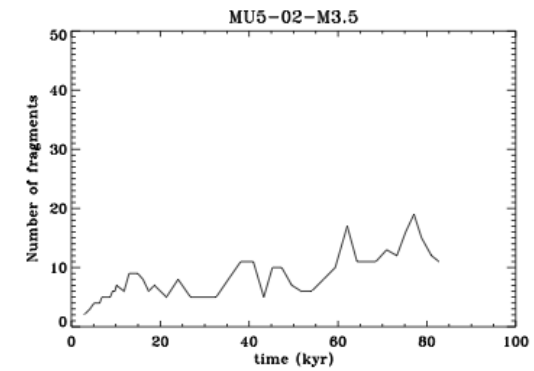
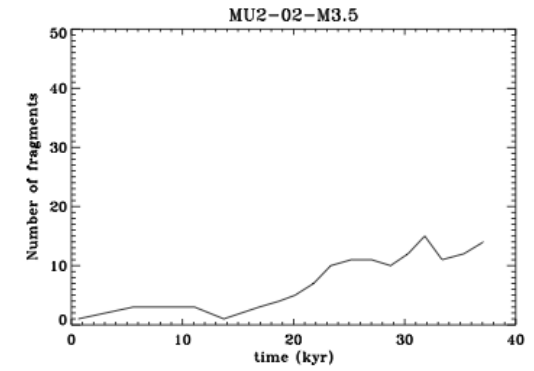
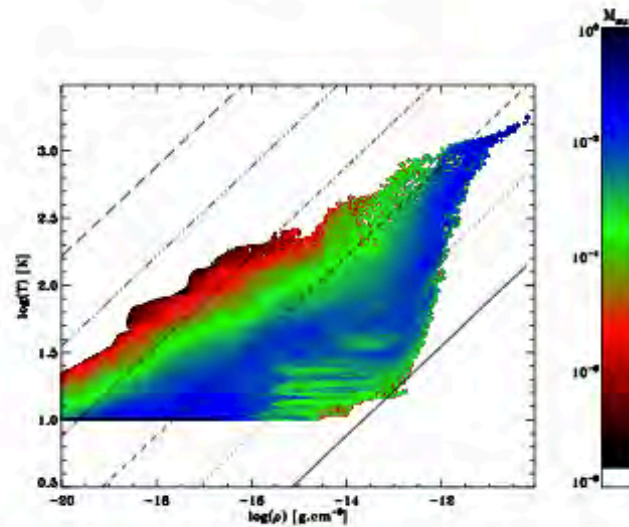
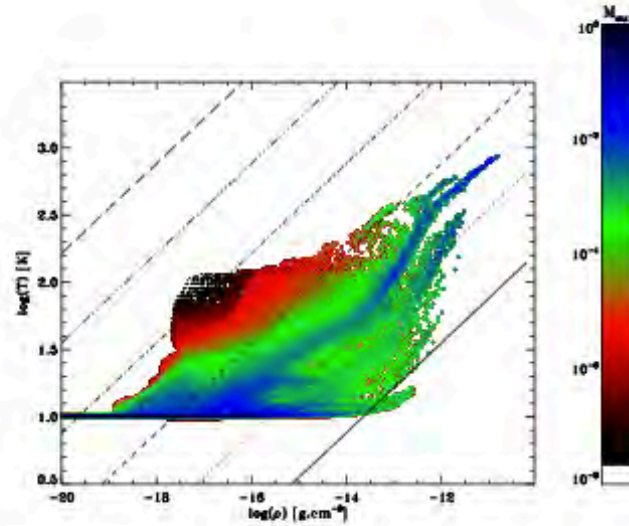
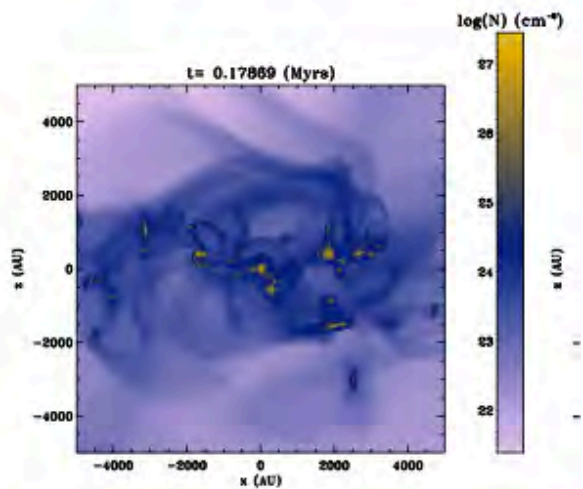
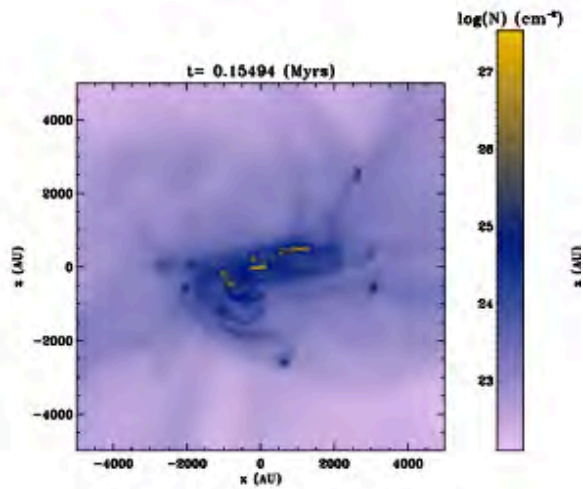
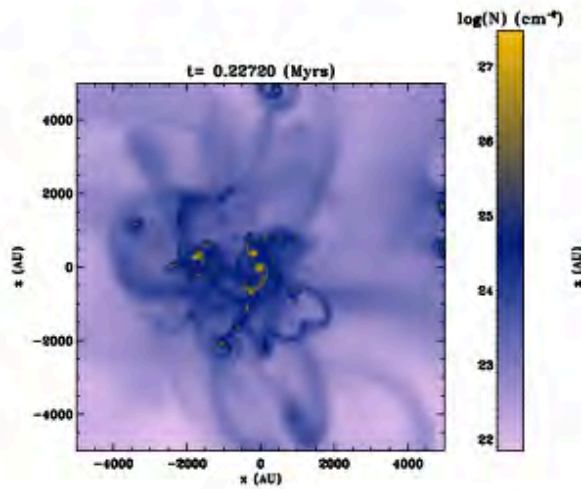
# 100 M<sub>⊙</sub> turbulent dense core collapse

Trend confirmed with lower resolution runs:



# 100 Ms cores with larger column densities

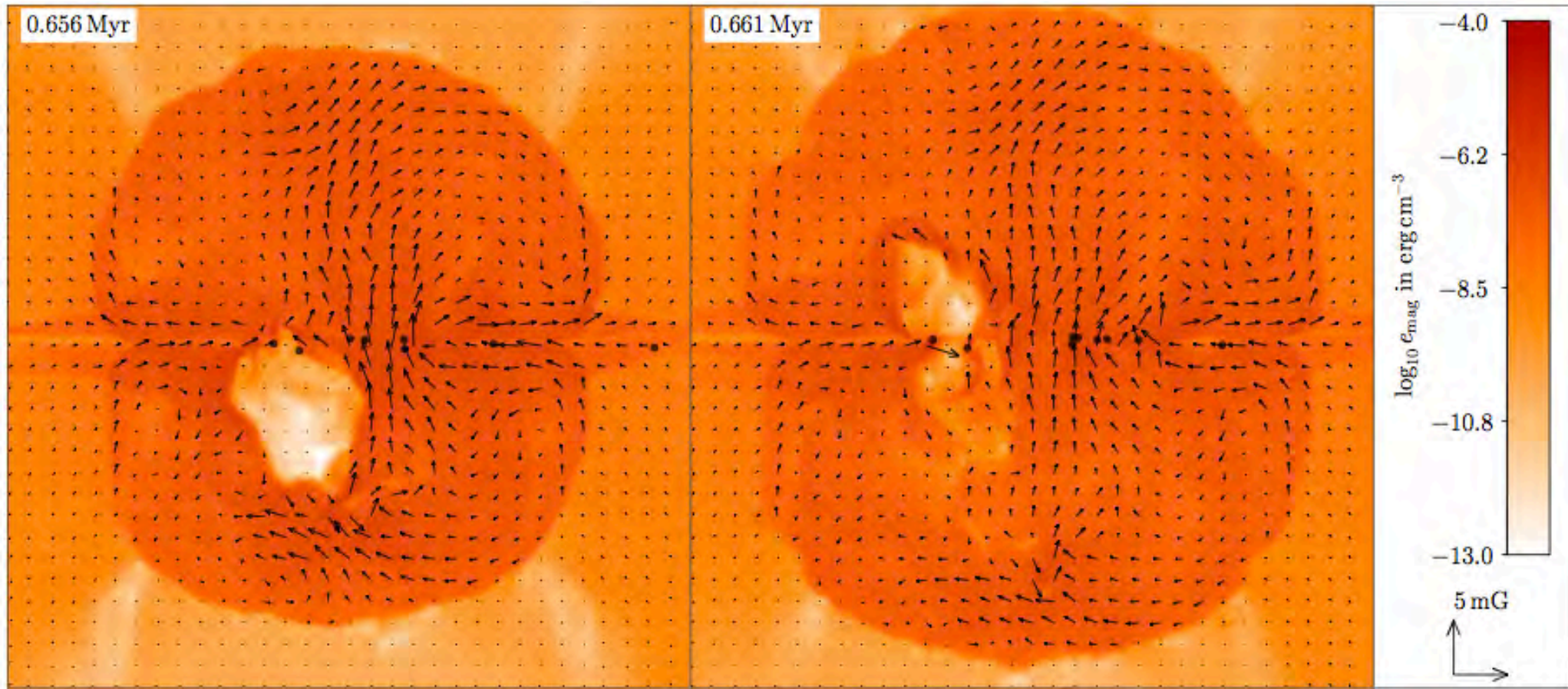
(Myers et al. 2014, Commercon & H 2015)



Similar effects still observed  
Magnetized runs have about 2 times less fragments

Peters et al. 2010, 2011, 2012

take also into account **ionising radiation**



Ionising radiation tends to push further the gas outwards and may be important/dominant for outflows in massive stars

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# Competitive accretion : individual wells are unimportant

(Zinnecker 1982, Bonnell et al. 2001, Bate et al. 2003,...)

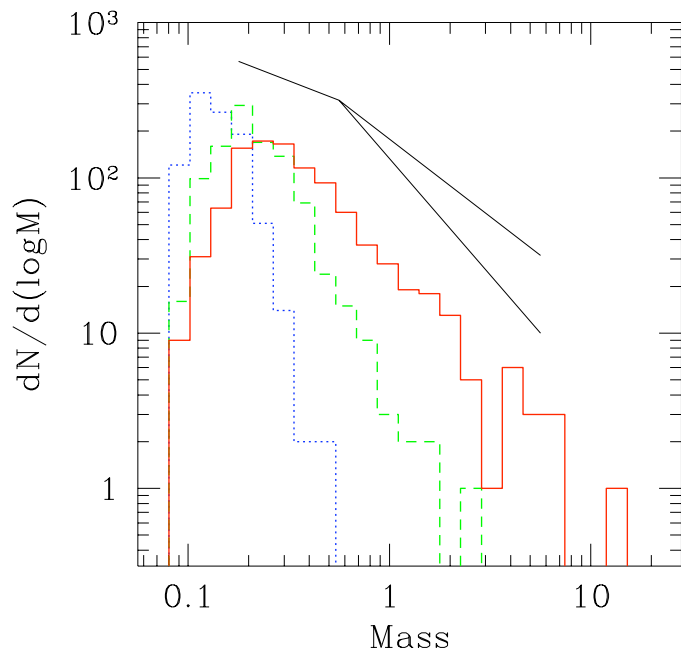
Stellar dominated Potential:  $\frac{dN}{dM} \propto M^{-2}$

Assume  $\rho_{gas} \propto R^{-3/2}$  : typical after rarefaction wave propagates away  
(Shu 1977)  $\dot{M}_* = \pi \rho V_{rel} R_{acc}^2$

$$R_{acc} \approx R_{BH} \approx \frac{GM_*}{V_{rel}^2}, \quad V_{rel} \approx \sqrt{GM_{cluster}/R} \approx R^{-1/2}$$

$\Rightarrow \dot{M}_* \propto M_*^2$  (accretion independent on the position in the cluster)

$\Rightarrow dN \propto M_*^{-2} dM_*$  (under reasonable assumptions...)



Mass spectrum from Bonnell et al. (2001)

1000 stars initially of mass 0.1 Ms, 10% of the total Mass

The mass spectrum develops and lead to a Salpeter type Slope

# How massive stars form ?

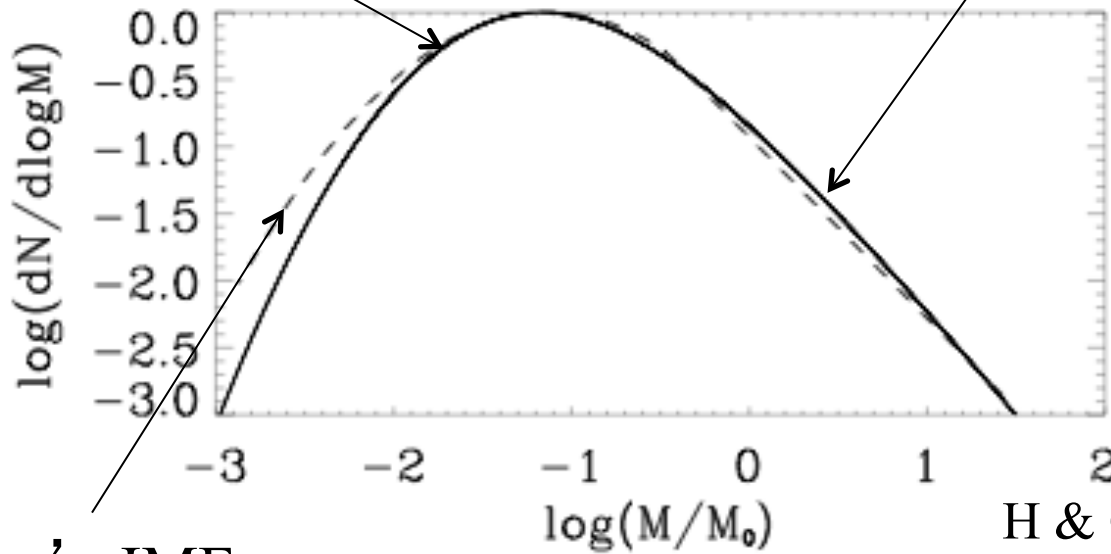
- Can we form massive stars in spite of the radiative pressure ?
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# Theories assuming that individual wells are determinant

(Padoan et al. 97, McKee & Tan 2003, H & Chabrier 2008, Hopkins 2012)

Thermal support  
Turbulent compression  
+ gravity

Turbulent dispersion  
Turbulent compression  
+ gravity



Chabrier's IMF

H & Chabrier 08

$$\mathcal{N}(\tilde{M}) = 2\mathcal{N}_0 \frac{1}{\tilde{R}^3} \frac{1}{1 + (2\eta + 1)\mathcal{M}_*^2 \tilde{R}^{2\eta}} \left[ \frac{1 + (1 - \eta)\mathcal{M}_*^2 \tilde{R}^{2\eta}}{(1 + \mathcal{M}_*^2 \tilde{R}^{2\eta})^{3/2}} - \frac{\delta_R^c + \sigma^2/2}{(1 + \mathcal{M}_*^2 \tilde{R}^{2\eta})^{1/2}} \frac{n' - 3}{4} \frac{\sigma_0^2}{\sigma^2} \left(\frac{\tilde{R}}{\tilde{L}_i}\right)^{n'-3} \right]$$

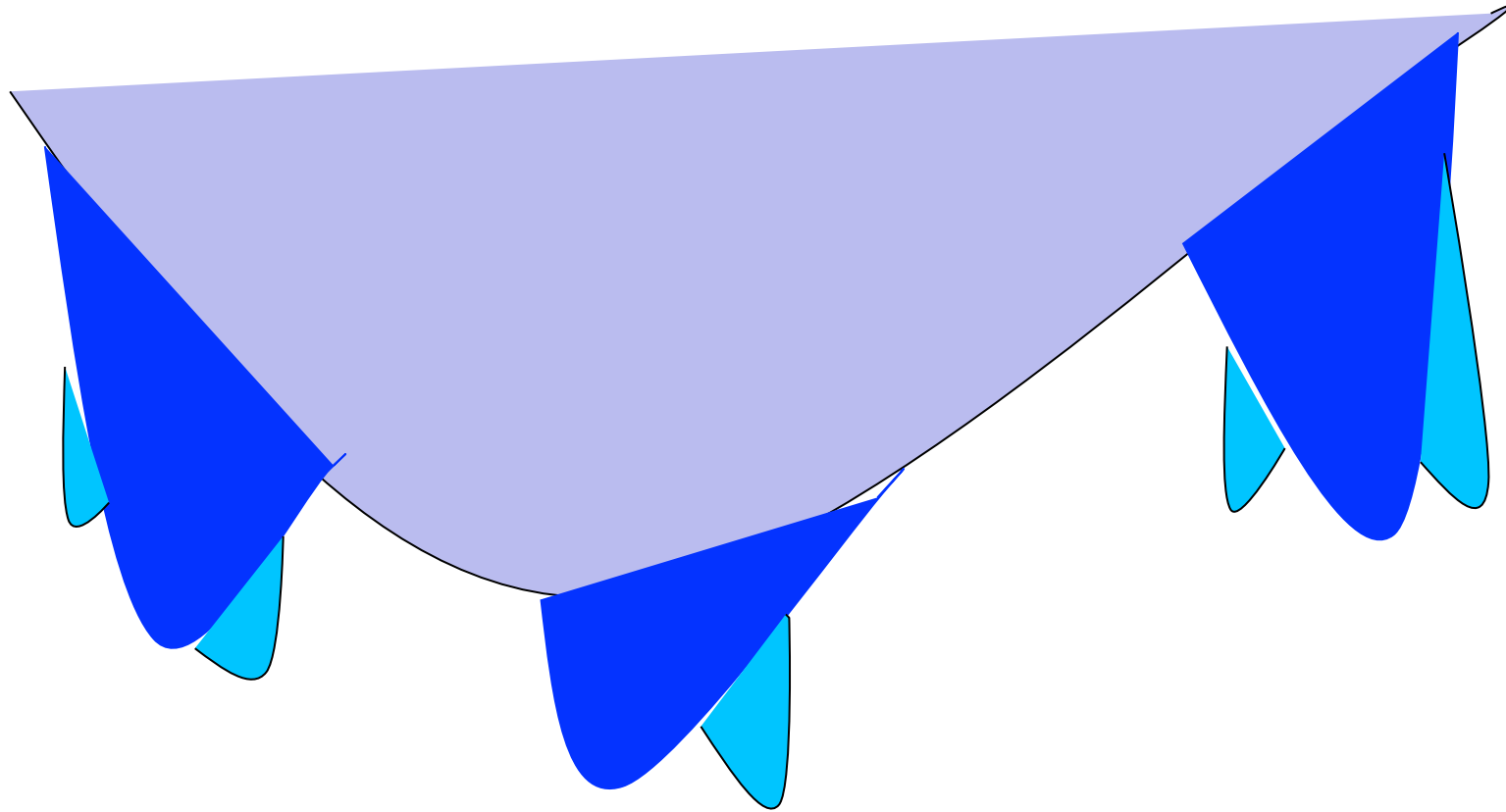
$$\times \exp\left\{ -\frac{[\ln(\tilde{M}/\tilde{R}^3)]^2}{2\sigma^2} \right\} \frac{\exp(-\sigma^2/8)}{\sqrt{2\pi}\sigma},$$



# How massive stars form ?

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## A hierarchy of wells:



Direct mapping between the wells and the stars ?  
Exchange between the wells ?  
Likely both ! But how much ?

# Which mechanism is at play in gravo-turbulent simulations ?

## Competitive accretion or core formation ?

Smith et al. have run SPH simulations with gravity and sink particles

They identify cores and look at the correlation between the core masses and the sink masses.

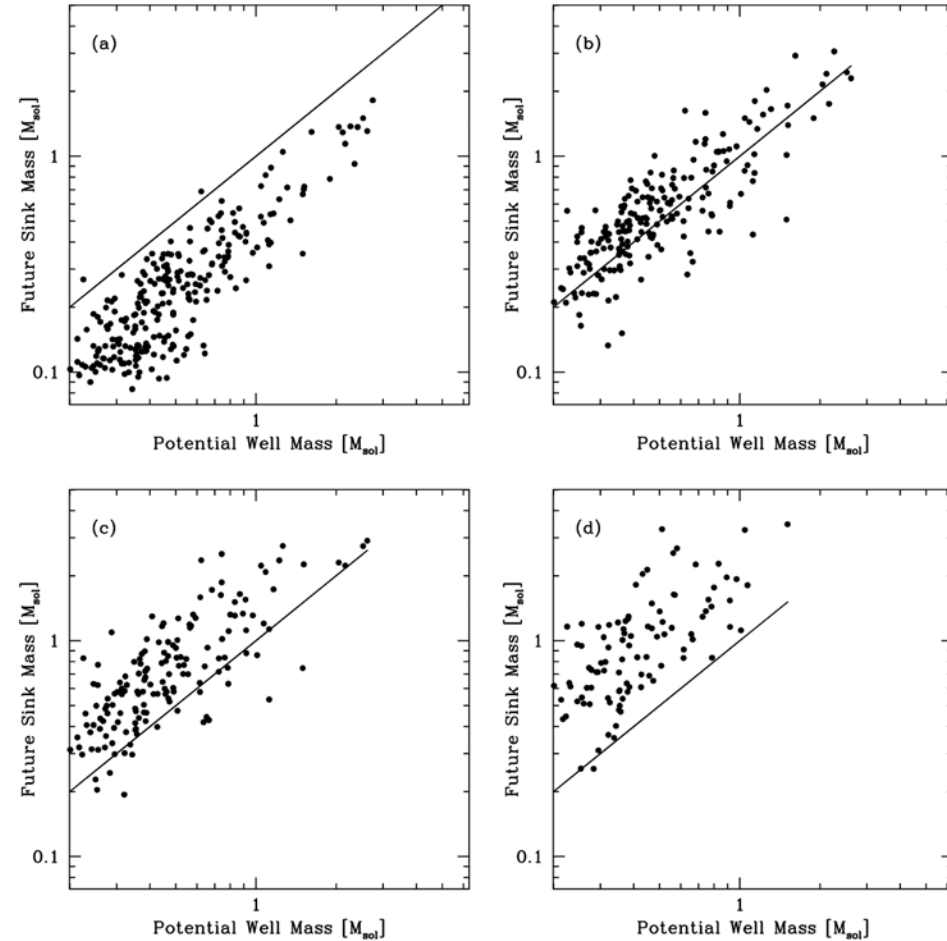
The correlation is very good initially (few freefall times) and becomes progressively less good.

*=> This is compatible with the core mass function being able to produce a reasonable IMF (Chabrier & H 2010).*

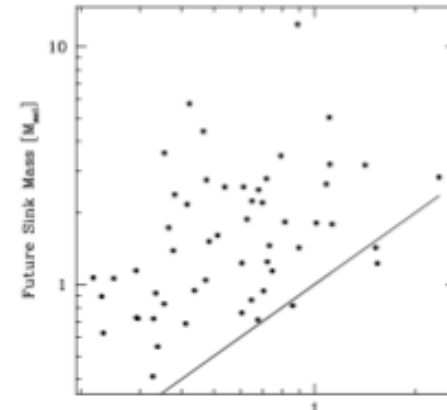
Until how many freefall times are the cores accreting ?

The most massive stars is more massive than the mass contains in its initial well.  
Where this mass comes from ?

Smith et al. 2008

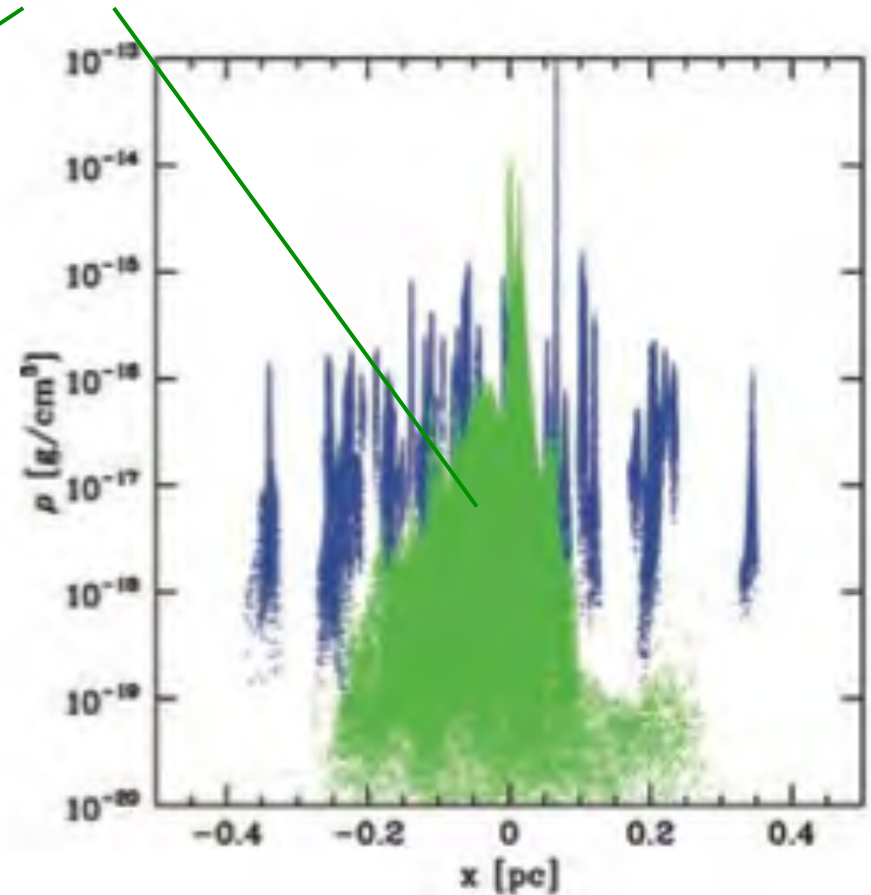
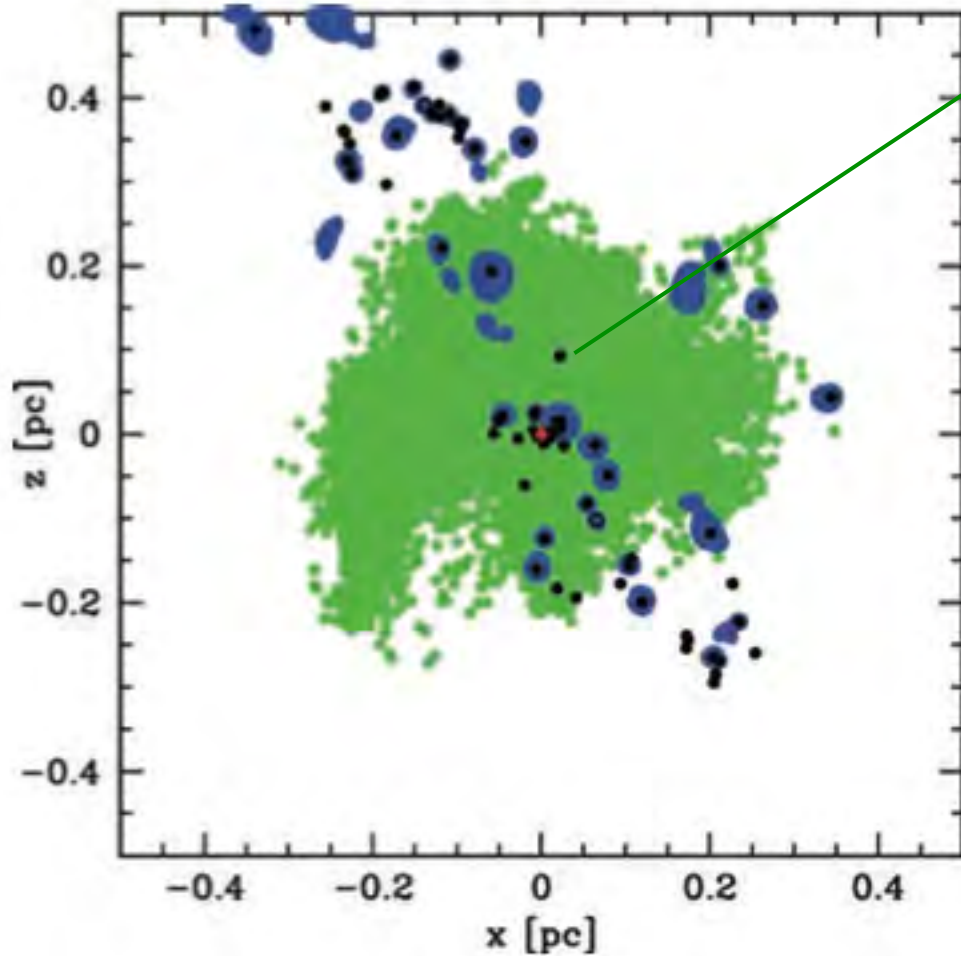


At the end of the simulation

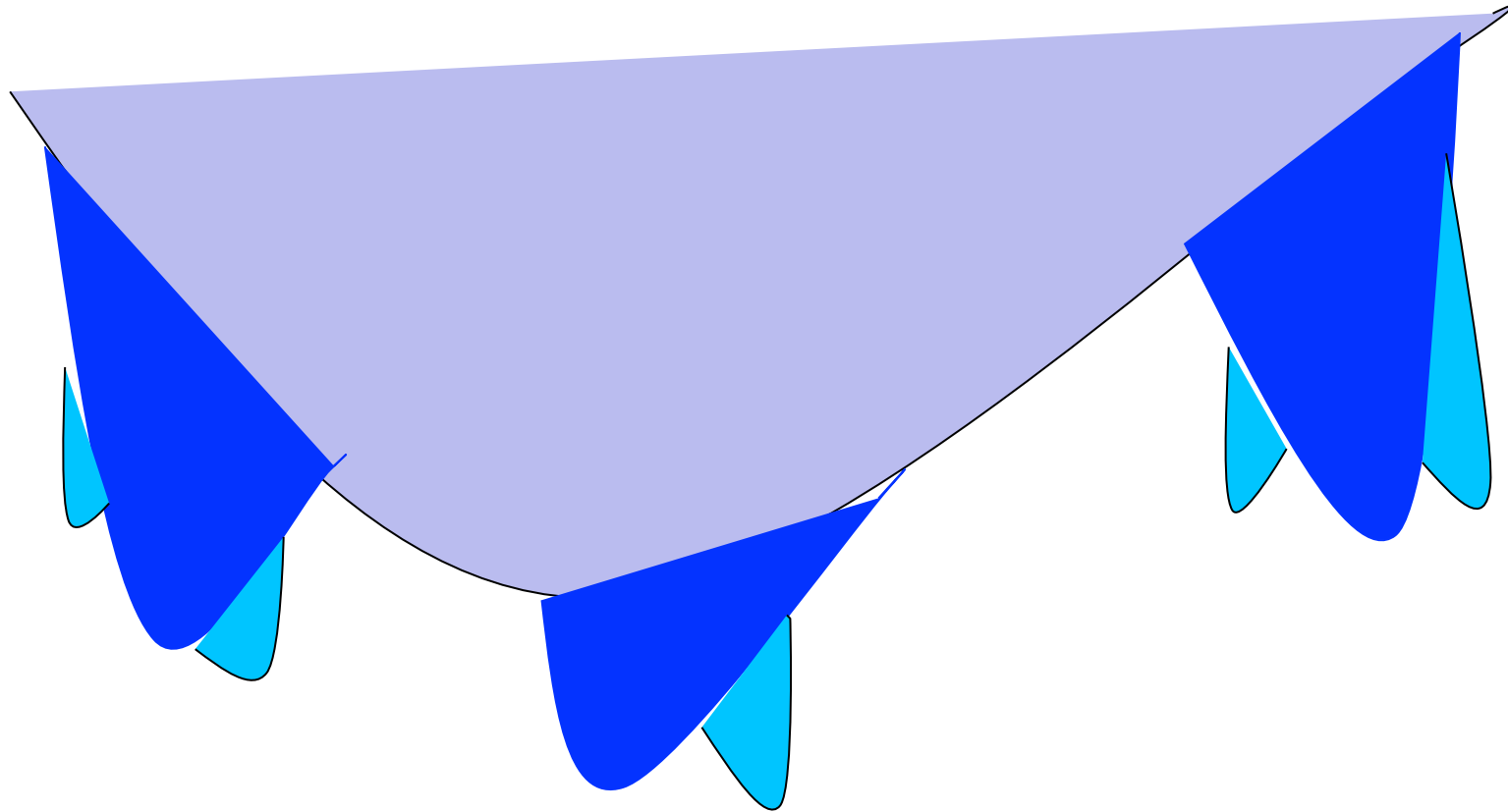


## Where the gas comes from ?

Green gas eventually falls in the massive star



## A hierarchy of wells:



Direct mapping between the wells and the stars ?  
Exchange between the wells ?  
Likely both ! But how much ?

# Conclusions

Impact of radiative transfer and magnetic field are obviously drastic in:

- regulating the mass accretion (but not stopping it)
- limiting the fragmentation

**Combination** of magnetic field and radiative transfer is **more** than their **mere** juxtaposition.

Where the mass is coming from ? still unclear.

=> **Accretion is not a sufficiently clear statement.**

The salient questions are:

- is accretion determined by the present mass object (compet. accret.) ?
- is accretion determined by the initial well hierarchy ?

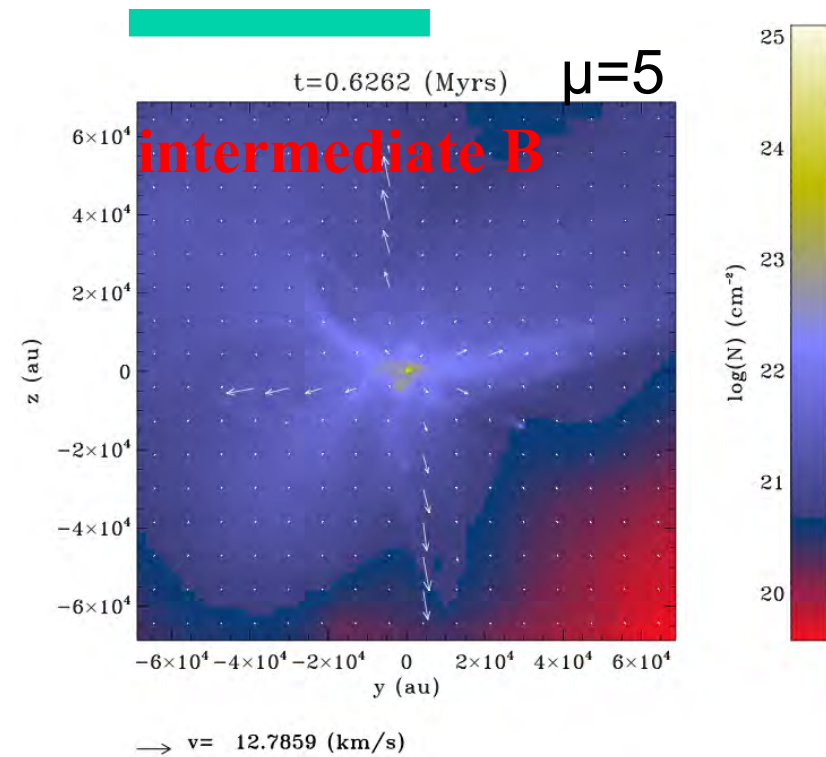
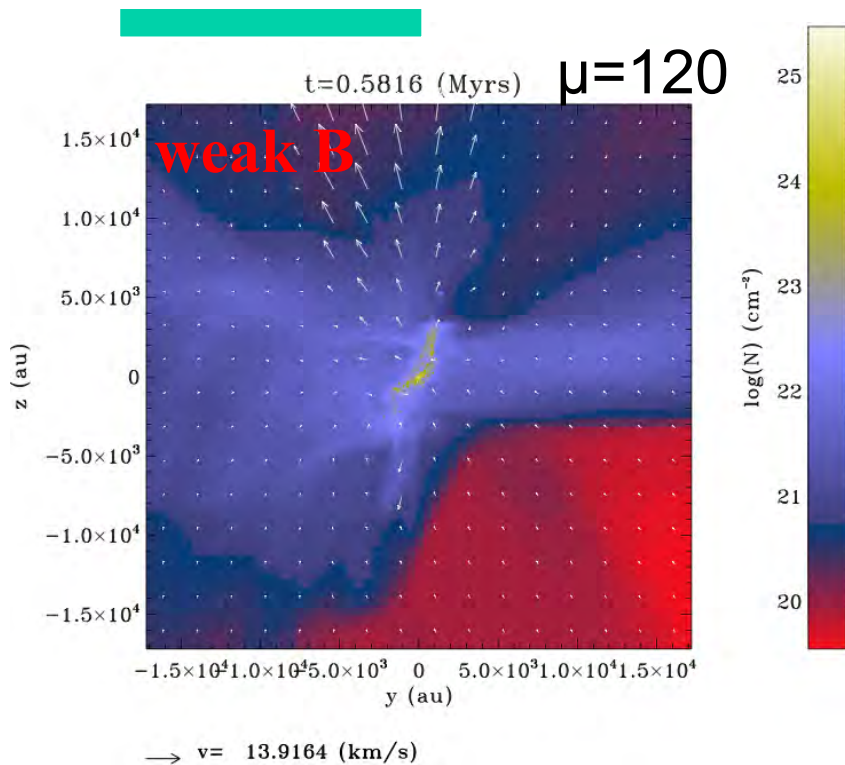
The feedback from massive stars is very non-linear. But predicting masses with an accuracy better than  $\sim 2$  is a **huge challenge**.

=> a huge multi-scale, multi-physics problems

# 100 M<sub>⊙</sub> magnetized, turbulent and dense barotropic core

Powerful outflows are launched even in turbulent cores

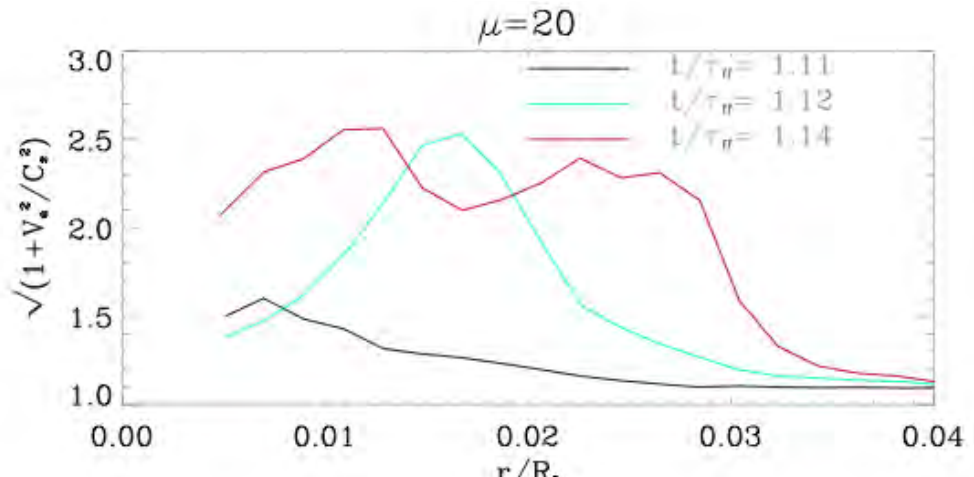
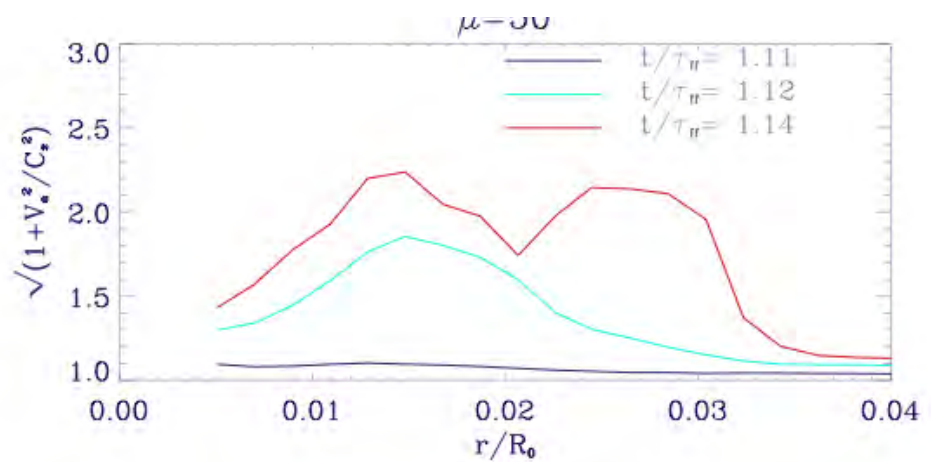
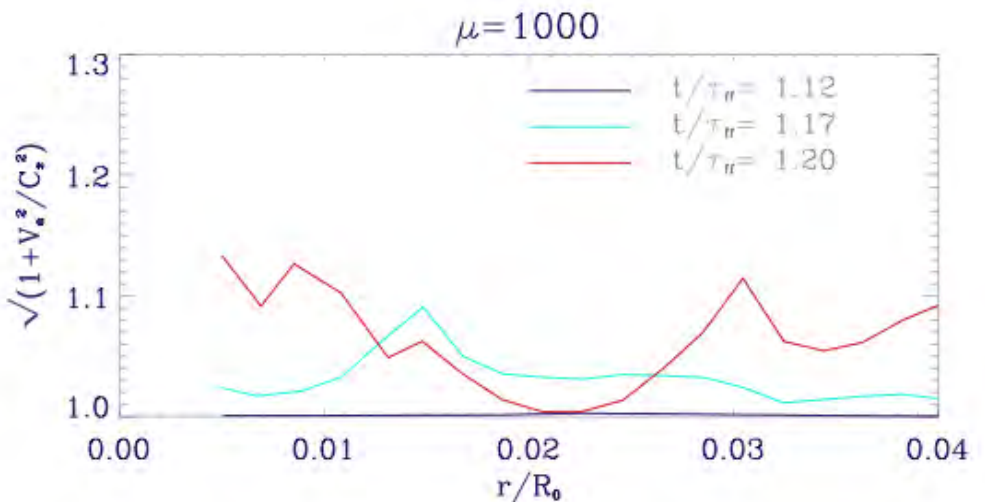
Faster flows appear with weaker fields



# Growth of the toroidal magnetic field within the disk

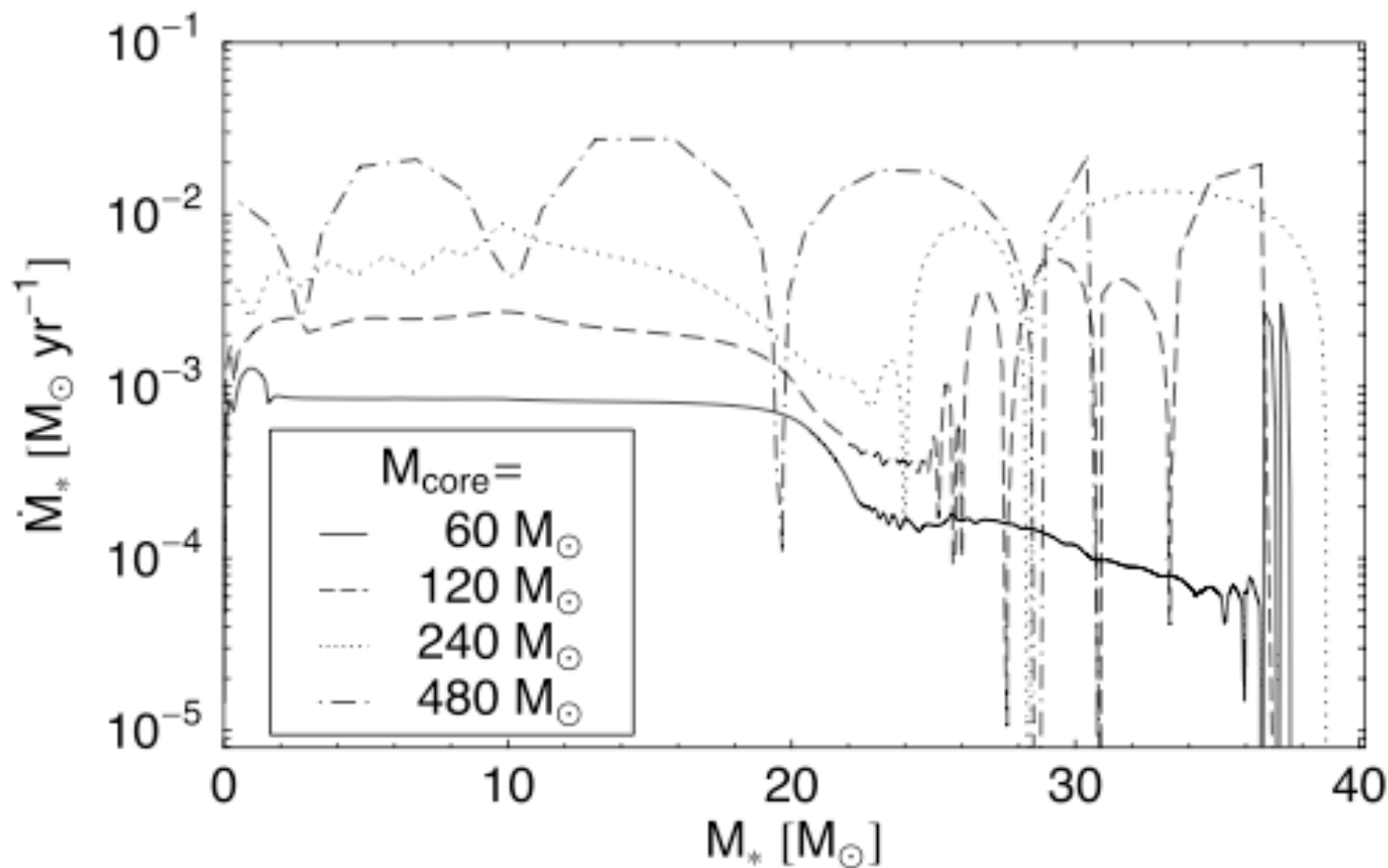
Importance of  $V_a/C_s$  for various  $\mu$  and various times

=>Compatible with the assumption that the toroidal field, stabilizes the disk.





# 1D results by Kuiper et al. (2010)



The final mass of the stars is about 35-37  $M_\odot$ .  
The history depends on the core mass.